

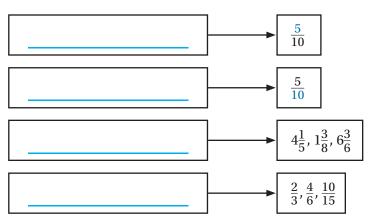
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#### Visualize It

Match the review words with their examples.

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What is it?
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What are some examples?



#### Understand Vocabulary

Complete the sentences by using the review words.

- **1.** A \_\_\_\_\_\_ is a number that is made up of a whole number and a fraction.
- **2.** The number below the bar in a fraction that tells how many equal parts are in the whole or in the group is the
- **3.** The \_\_\_\_\_\_ is the answer to a multiplication problem.
- 4. Fractions that name the same amount or part are called

5. The \_\_\_\_\_\_ is the number above the bar in a fraction that tells how many equal parts of the whole are being considered.



#### **Connect to Vocabulary**

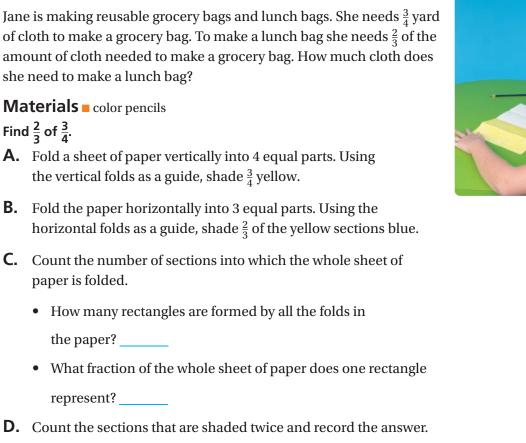
#### Review Words

denominator equivalent fractions mixed number numerator product

### **Multiply Fractions**

**I Can** use visual models to show the product of two fractions.

### Investigate

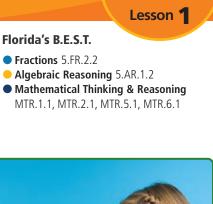


$$\frac{2}{3} \times \frac{3}{4} =$$
\_\_\_\_\_

So, Jane needs \_\_\_\_\_\_ yard of cloth to make a lunch bag.

### **Draw Conclusions**

- **1.** Explain why you shaded  $\frac{2}{3}$  of the yellow sections blue rather than shading  $\frac{2}{3}$  of the whole.
- **2. MTR** Analyze what you are finding if a model shows  $\frac{1}{2}$  of a sheet of paper shaded yellow and  $\frac{1}{3}$  of the yellow section shaded blue.



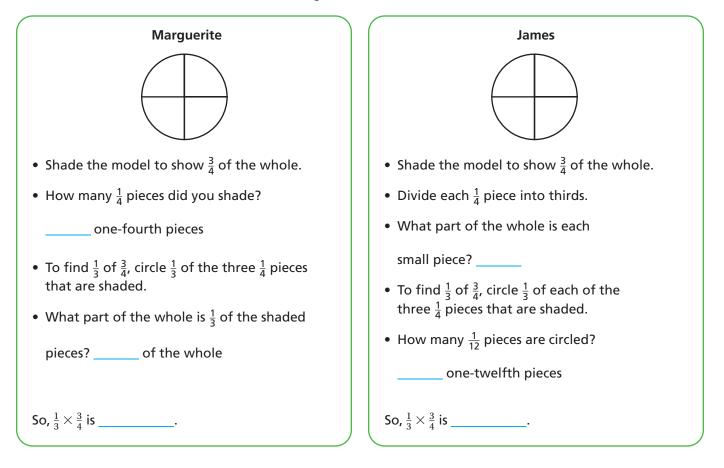
**CHAPTER 10** 



### **Make Connections**

You can find a part of a part in different ways. Marguerite and James both correctly solved the problem  $\frac{1}{3} \times \frac{3}{4}$  using the steps shown.

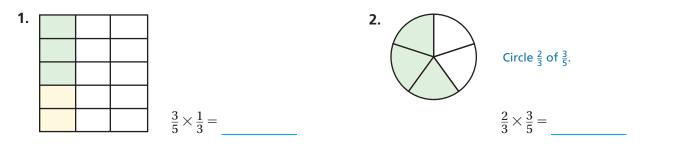




• Pose a problem that can be solved using the expression above.

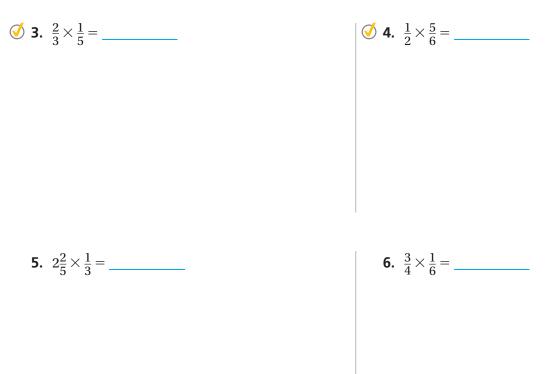
# Share and Show Math Board

Use the model or *i*Tools to find the product.



#### Name

Find the product. Draw a model.



### **On Your Own**

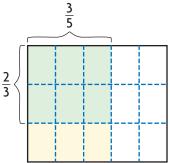
7. **MTR** Ricardo's recipe for 4 loaves of bread requires  $\frac{2}{3}$  cup of olive oil. He only wants to make 1 loaf. Ricardo makes a model to find out how much oil he needs to use. He folds a piece of paper vertically into three parts and shades two parts. Then he folds the paper horizontally into four parts and shades  $\frac{1}{4}$  of the shaded part. Ricardo decides he needs  $\frac{1}{4}$  cup of olive oil. Is he right? Explain.

8. Three-fourths of a spinach casserole is left over after Sam has lunch. Jackie and Alicia each take  $\frac{1}{2}$  of the leftover casserole. Jackie eats only  $\frac{2}{3}$  of her portion. What fraction of a whole casserole did Jackie eat? Draw a model.

#### What's the Error?

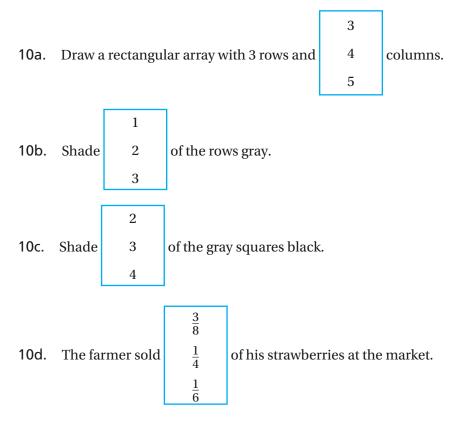
**9.** Cheryl and Marcus are going to make 2 batches of muffins. The smaller batch is  $\frac{2}{3}$  the size of the larger batch. The recipe for the larger batch requires  $\frac{3}{5}$  cup of water. How much water will they need to make the smaller batch?





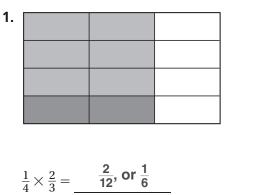
They made a model to represent the problem. Cheryl says they need  $\frac{6}{9}$  cup of water. Marcus says they need  $\frac{6}{15}$  cup of water. Who is correct? Explain.

**10.** A farmer took  $\frac{2}{3}$  of the strawberries that he harvested to a market. At the market, the farmer sold  $\frac{1}{4}$  of the strawberries. How can you find what part of the harvested strawberries were sold at the market? For 10a–10d, choose the number that makes each sentence true.



### **Multiply Fractions**

#### Find the product.





#### Find the product. Draw a model.

- **3.**  $\frac{4}{5} \times \frac{1}{2} =$
- **5.**  $\frac{3}{8} \times \frac{2}{3} =$

# Problem Solving 🔛

- 7. Nora has a piece of ribbon that is  $\frac{3}{4}$  yard long. She will use  $\frac{1}{2}$  of it to make a bow. What length of the ribbon in yards will she use for the bow?
- 8. Marlon bought  $\frac{7}{8}$  pound of turkey at the deli. He used  $\frac{2}{3}$  of it to make sandwiches for lunch. How much turkey in pounds did Marlon use for sandwiches?

#### LESSON 10.1 Practice and Homework

#### Go Online

Interactive Examples



 $\frac{2}{5} \times \frac{5}{6} = \underline{\qquad}$ 

2.

```
6. \frac{3}{5} \times \frac{3}{5} =
```

### **Lesson Check**

- **9.** Tina has  $\frac{3}{5}$  pound of rice. She will use  $\frac{2}{3}$  of it to make fried rice for her family. How much rice in pounds will Tina use to make fried rice?
- **10.** The Waterfall Trail is  $\frac{3}{4}$  mile long. At  $\frac{1}{6}$  of the distance from the trailhead, there is a lookout. In miles, how far is the lookout from the trailhead?

### **Spiral Review**

- **11.** Hayden bought 48 new trading cards. Threefourths of the new cards are baseball cards. How many baseball cards did Hayden buy?
- **12.** Yesterday, Deja walked  $\frac{9}{10}$  mile to her friend's house. Together, they walked  $\frac{1}{3}$  mile to the library. What is a reasonable estimate for how far Deja walked yesterday?

- **13.** Vy is going to sew a jacket and a skirt. She needs  $2\frac{3}{4}$  yards of material for the jacket and  $1\frac{1}{2}$  yards of material for the skirt. Altogether, how many yards of material does Vy need?
- **14.** Use properties to solve.

$$(3 \times 6) + (5 \times 2) \div 7$$

# **Compare Relative Size of Products** to Fraction Factors

**I Can** compare the size of a product to the size of one factor when multiplying fractions.

### 🔡 UNLOCK the Problem

Multiplication can be thought of as resizing one number by another number. For example,  $2 \times 3$  will result in a product that is 2 times as great as 3.

What happens to the size of a product when a number is multiplied by a fraction rather than a whole number?

**One Way** Use a model.

**A** During the week, the Delgado family ate  $\frac{3}{4}$  of a box of cereal.

- Shade the model to show  $\frac{3}{4}$  of a box of cereal.
- Write an expression for  $\frac{3}{4}$  of 1 box of cereal.  $\frac{3}{4} \times$
- Will the product be equal to, greater than, or less than 1?
- **B** The Ling family has 4 boxes of cereal. They ate  $\frac{3}{4}$  of all the cereal during the week.
  - Shade the model to show  $\frac{3}{4}$  of 4 boxes of cereal.
  - Write an expression for  $\frac{3}{4}$  of 4 boxes of cereal.  $\frac{3}{4} \times$
  - Will the product be equal to, greater than, or less than 4?
- **C** The Carter family has only  $\frac{1}{2}$  of a box of cereal at the beginning of the week. They ate  $\frac{3}{4}$  of the  $\frac{1}{2}$  box of cereal.
  - Shade the model to show  $\frac{3}{4}$  of  $\frac{1}{2}$  box of cereal.
  - Write an expression to show  $\frac{3}{4}$  of  $\frac{1}{2}$  box of cereal.  $\frac{3}{4} \times$
  - Will the product be equal to, greater than, or less than  $\frac{1}{2}$ ? than  $\frac{3}{4}$ ?



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- Fractions 5.FR.2.3
- Algebraic Reasoning 5.AR.1.2
- Mathematical Thinking & Reasoning MTR.1.1, MTR.3.1, MTR.4.1, MTR.5.1, MTR.6.1

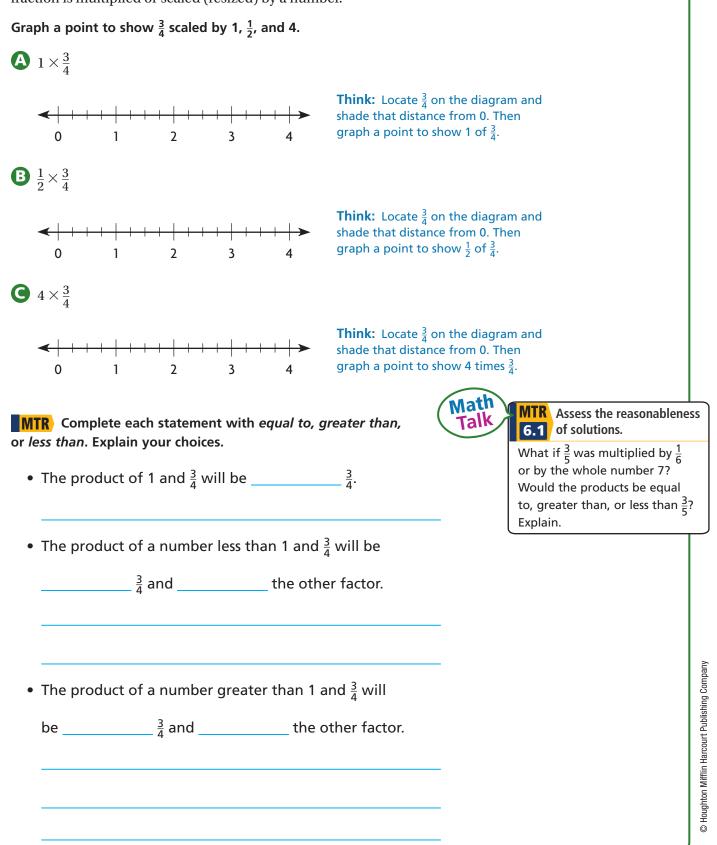




Lesson 2

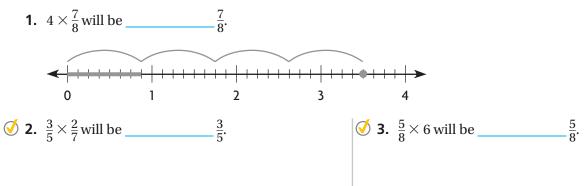
#### Another Way Use a diagram.

You can use a diagram to show the relationship between the products when a fraction is multiplied or scaled (resized) by a number.



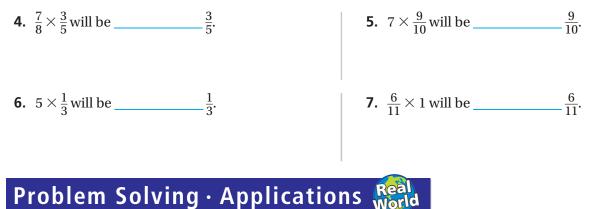
### Share and Show Math Board

Complete the statement with equal to, greater than, or less than.



### On Your Own

Complete the statement with equal to, greater than, or less than.



- **8.** Rashid is planning on spending  $\frac{2}{3}$  as many hours watching television this week as he did last week.
  - Is Rashid going to spend more hours or fewer hours watching television this week?
- **9.** Mrs. Rodriguez has 18 packages of pens in stock at her store on Monday. On Tuesday, she has  $\frac{5}{6}$  the number of pens she had on Monday. On Wednesday, she has  $\frac{2}{5}$  of the number of pens she had on Tuesday. How many packages of pens does she have on Wednesday?
- **10.** MTR Ariel goes running for  $\frac{5}{6}$  of an hour. The next day, she runs for  $\frac{3}{4}$  as much time. Does she spend more or less time running the second day? Draw a diagram or make a model to represent the problem.

#### **Connect to Art**

A scale model is a representation of an object with the same shape as the real object. Models can be larger or smaller than the actual object, but are often smaller.

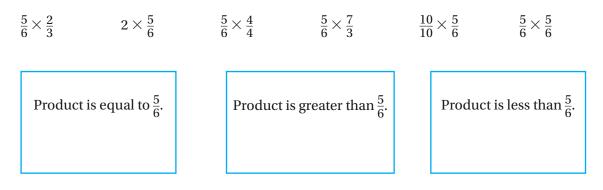
Architects often make scale models of the buildings or structures they plan to build. Models can give them an idea of how the structure will look when finished. Each measurement of the building is scaled up or down by the same factor.

Bob is building a scale model of his bike. He wants his model to be  $\frac{1}{5}$  as long as his bike.

- **11.** If Bob's bike is 60 inches long, how long will his model be?
- **12.** If one wheel on Bob's model is 4 inches across, how many inches across is the actual wheel on his bike? Explain.



**13.** Write each multiplication expression in the correct box.



9. **WRITE** Math Explain how you can compare the size of a product to the size of a factor when multiplying fractions without actually doing the multiplication. Include a model.

7. Shani is making hot cocoa. She plans to multiply the recipe by 4 to make enough hot cocoa for the whole class. If the recipe calls for  $\frac{1}{2}$  teaspoon vanilla extract, will she need more than  $\frac{1}{2}$  teaspoon or less than  $\frac{1}{2}$  teaspoon of vanilla extract to make all the hot cocoa?

Think:  $\frac{4}{7}$  is multiplied by a

so,  $\frac{3}{5} \times \frac{4}{7}$  will be less than  $\frac{4}{7}$ .

number less than 1;

- Problem Solving Real
- **5.**  $\frac{4}{9} \times \frac{3}{8}$  will be \_\_\_\_\_\_ **6.**  $\frac{4}{5} \times \frac{7}{7}$  will be \_\_\_\_\_\_

**1.**  $\frac{3}{5} \times \frac{4}{7}$  will be \_\_\_\_\_\_ **2.**  $5 \times \frac{7}{8}$  will be \_\_\_\_\_\_

- $\frac{4}{5}$ .
- **8.** Miles is planning to spend  $\frac{2}{3}$  as many hours cycling this week as he did last week. Is Miles going to spend more hours or fewer hours cycling this week than last week?

**Compare Relative Size of Products to Fraction Factors** 

Complete the statement with equal to, greater than, or less than.

Name

**LESSON 10.2 Practice and Homework** 

 $\frac{7}{8}$ .

**Go Online** 

**Interactive Examples** 

### **Lesson Check**

- **10.** Trevor saves  $\frac{2}{3}$  of the money he earns at his after-school job. Suppose Trevor starts saving  $\frac{1}{4}$  as much as he is saving now. Will he be saving less, more, or the same amount?
- **11.** Suppose you multiply a whole number greater than 1 by the fraction  $\frac{3}{5}$ . Will the product be greater than, less than, or equal to  $\frac{3}{5}$ ?

#### **Spiral Review**

- **12.** In the next 10 months, Kai wants to save \$900 for his vacation. He plans to save \$75 each of the first 8 months. How much must he save each of the last 2 months in order to meet his goal if he saves the same amount each month?
- **13.** What is the total cost of 0.5 pound of peaches selling for \$0.80 per pound and 0.7 pound of oranges selling for \$0.90 per pound?

- **14.** Cerise hiked 15.12 miles in 6.3 hours. If Cerise hiked the same number of miles each hour, how many miles did she hike each hour?
- **15.** It is  $42\frac{1}{2}$  miles from Eaton to Baxter, and  $37\frac{4}{5}$  miles from Baxter to Wellington. How far is it from Eaton to Wellington, if you go by way of Baxter?

# **Compare Relative Size of Products** with Fraction Multiplication

**I Can** multiply fractions and explain how the size of a product compares to the size of the factors.

### 🗄 UNLOCK the Problem

Sasha has  $\frac{3}{5}$  of a scarf left to knit. If she finishes  $\frac{1}{2}$  of that today, how much of the scarf will Sasha knit today? **Multiply.**  $\frac{1}{2} \times \frac{3}{5}$ 

#### **One Way** Use a model.

- Shade  $\frac{3}{5}$  of the model yellow.
- Draw a horizontal line across the rectangle to show 2 equal parts.
- Shade  $\frac{1}{2}$  of the yellow sections blue.
- Count the sections that are shaded twice and write a fraction for the parts of the whole that are shaded twice.



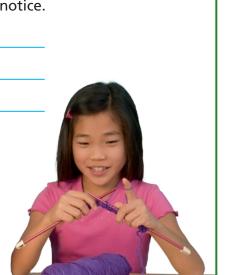
• Compare the numerator and denominator of the product with the numerators and denominators of the factors. Describe what you notice.

### Another Way Use paper and pencil.

You can multiply fractions without using a model.

- Multiply the numerators.
- Multiply the denominators.

$$\frac{1}{2} \times \frac{3}{5} = \frac{1 \times 1}{2 \times 1}$$



• How much of the scarf does Sasha have left

Of the fraction that is left, how much will she

to knit?

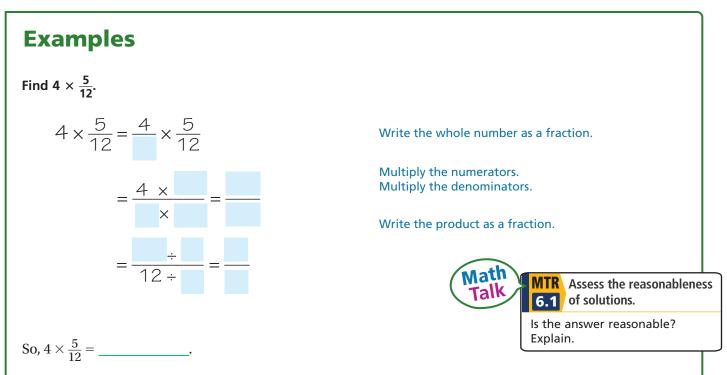
finish today?

- Algebraic Reasoning 5.AR.1.2
- Mathematical Thinking & Reasoning
- MTR.2.1, MTR.4.1, MTR.5.1, MTR.6.1

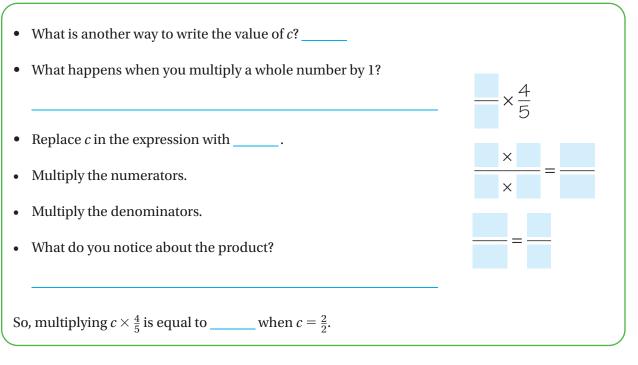
So, Sasha will knit \_\_\_\_\_ of the scarf today.

Lesson 3

**MTR** Remember you can write a whole number as a fraction with a denominator of 1.



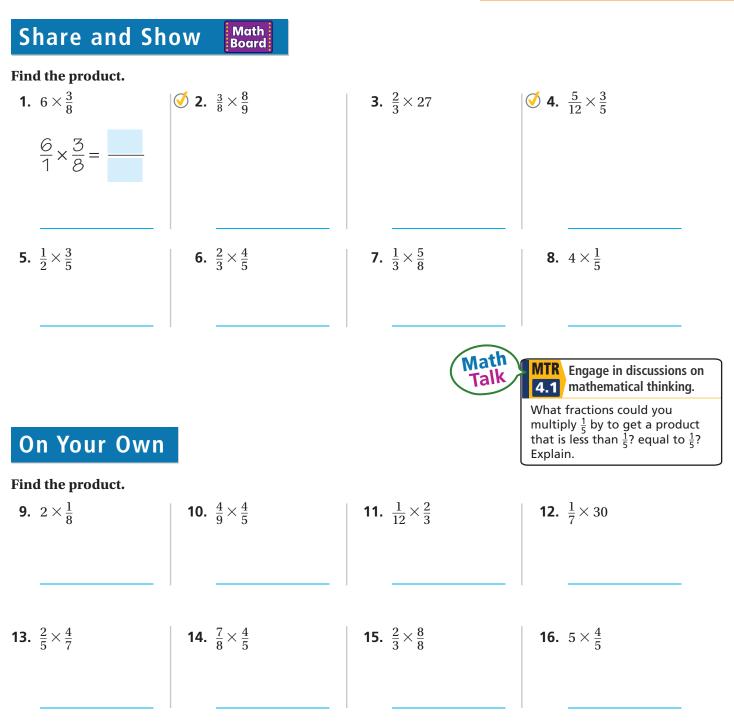
#### **Try This!** Evaluate $c \times \frac{4}{5}$ for $c = \frac{2}{2}$ .



• **MTR** Will you get the same result if you multiply  $\frac{4}{5}$  by any fraction with a numerator and denominator that are the same digit? Explain.

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- **17.** Of the pets in the pet show,  $\frac{5}{6}$  are cats.  $\frac{4}{5}$  of the cats are calico cats. What fraction of the pets are calico cats?
- **18.** Five cats each ate  $\frac{1}{4}$  cup of canned food and  $\frac{1}{4}$  cup of dry food. How much food did they eat altogether?

# Problem Solving · Applications

Speed skating is a popular sport in the Winter Olympics. Many young athletes in the United States participate in speed-skating clubs and camps.

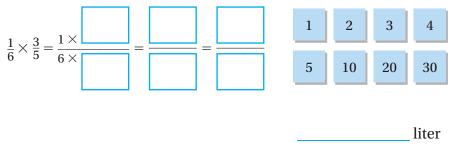
**19.** At a camp in Green Bay, Wisconsin,  $\frac{7}{9}$  of the participants were from Wisconsin. Of that group,  $\frac{3}{5}$  were 12 years old. What fraction of the group was from Wisconsin and 12 years old?



**20.** Maribel wants to skate  $1\frac{1}{2}$  miles on Monday. If she skates  $\frac{9}{10}$  mile Monday morning and  $\frac{2}{3}$  of that distance Monday afternoon, will she reach her goal? Explain.



- **21.** MTR On the first day of camp,  $\frac{5}{6}$  of the skaters were beginners. Of the beginners,  $\frac{1}{3}$  were girls. What fraction of the skaters were girls and beginners? Explain why your answer is reasonable.
- **22.** A scientist had  $\frac{3}{5}$  liter of solution. He used  $\frac{1}{6}$  of the solution for an experiment. How much solution in liters did the scientist use for the experiment? Use the numbers on the tiles to complete the calculations. You may use numbers more than once or not at all.



**6.** Ciara raked  $\frac{3}{5}$  of the yard. Minni raked  $\frac{1}{3}$  of the amount Karen raked. How much of the yard did Minni rake?

**Compare Relative Size of Products** 

**7.** In the pet show,  $\frac{3}{8}$  of the pets are dogs. Of the dogs,  $\frac{2}{3}$  have long hair. What fraction of the pets are dogs with long hair?

#### Algebra Evaluate for the given value of the variable.

**8.**  $\frac{7}{8} \times c$  for c = 8 **9.**  $t \times \frac{3}{4}$  for  $t = \frac{8}{9}$  **10.**  $\frac{1}{2} \times s$  for  $s = \frac{3}{10}$  **11.**  $y \times 6$  for  $y = \frac{2}{3}$ 

# Problem Solving Real

- **12.** Peja ran  $\frac{5}{7}$  of the distance around the school track. Sara ran  $\frac{4}{5}$  of Peja's distance. What fraction of the total distance around the track did Sara run?
- **13.** A group of students attend a math club. Half of the students are boys and  $\frac{4}{9}$  of the boys have brown eyes. What fraction of the group are boys with brown eyes?

**14. WRITE** *Math* Explain how multiplying fractions is similar to multiplying whole numbers and how it is different.

LESSON 10.3 Practice and Homework

### **Lesson Check**

- **15.** Som attended band practice for  $\frac{5}{6}$  hour. Then he went home and practiced for  $\frac{2}{5}$  as long as band practice. How many minutes did he practice at home?
- **16.** Vailea read  $\frac{5}{8}$  of a 56-page book. How many pages did Vailea read?

### **Spiral Review**

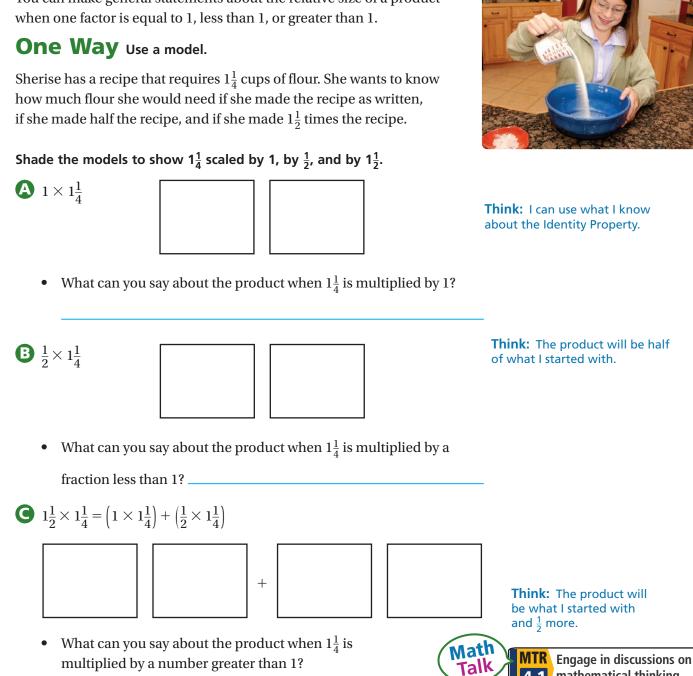
**17.** What is the quotient of  $\frac{18}{1,000}$ ?

**18.** A machine produces 1,000 bowling pins per hour, each valued at \$8.37. What is the total value of the pins produced in 1 hour?

- **19.** Keith had  $8\frac{1}{2}$  cups of flour. He used  $5\frac{2}{3}$  cups to make bread. How many cups of flour does Keith have left?
- **20.** The Blue Lake Trail is  $11\frac{3}{8}$  miles long. Gemma has hiked  $2\frac{1}{2}$  miles each hour for 3 hours. How far is she from the end of the trail?

# **Compare Relative Size of Products** to Mixed Number Factors

( I Can ) compare the size of a product to the size of one factor when multiplying fractions greater than one.



# UNLOCK the Problem

You can make general statements about the relative size of a product



**4.1** mathematical thinking.

Explain your answer to Part C.

**CHAPTER 10** 

#### Lesson **4**

- Fractions 5.FR.2.3
- Algebraic Reasoning 5.AR.1.2
- Mathematical Thinking & Reasoning MTR.1.1, MTR.2.1, MTR.4.1, MTR.5.1, MTR.6.1

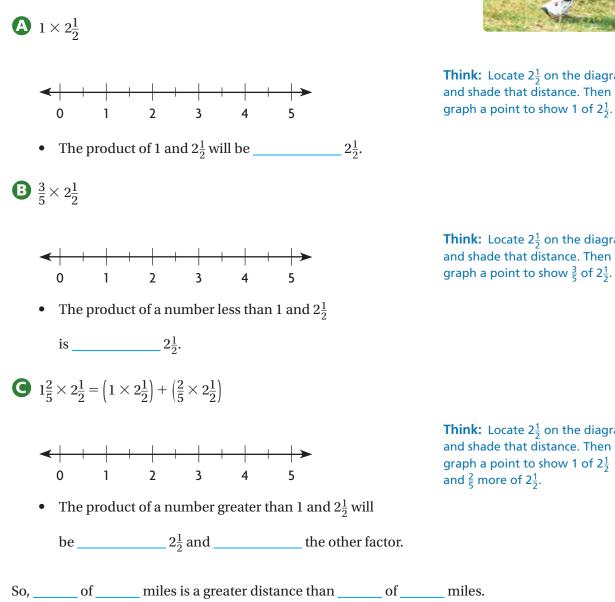
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MTR You can also use a diagram to show the relationship between the products when a fraction greater than one is multiplied or scaled (resized) by a number.

#### Another Way Use a diagram.

Venec wants to train for a road race. He plans to run  $2\frac{1}{2}$  miles on the first day. On the second day, he plans to run  $\frac{3}{5}$  of the distance he runs on the first day. On the third day, he plans to run  $1\frac{2}{5}$  of the distance he runs on the first day. Which distance is greater: the distance on day 2 when he runs  $\frac{3}{5}$  of  $2\frac{1}{2}$  miles, or the distance on day 3 when he runs  $1\frac{2}{5}$  of  $2\frac{1}{2}$  miles?

Graph a point on the diagram to show the size of the product. Then complete the statement with equal to, greater than, or less than.



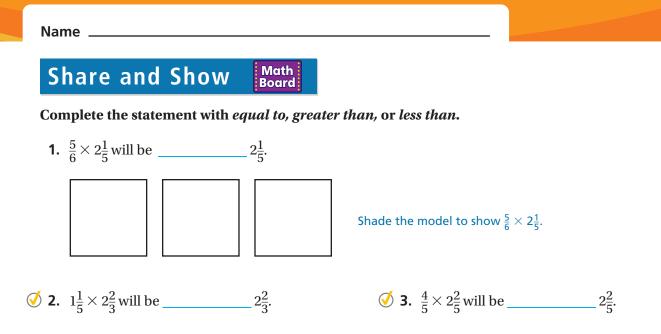


**Think:** Locate  $2\frac{1}{2}$  on the diagram

**Think:** Locate  $2\frac{1}{2}$  on the diagram

**Think:** Locate  $2\frac{1}{2}$  on the diagram

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### On Your Own

Complete the statement with equal to, greater than, or less than.

**4.**  $\frac{2}{2} \times 1\frac{1}{2}$  will be \_\_\_\_\_\_  $1\frac{1}{2}$ . **5.**  $\frac{2}{3} \times 3\frac{1}{6}$  will be \_\_\_\_\_\_  $3\frac{1}{6}$ .

**MTR** Tell whether the unknown factor is *less than 1* or greater than 1.

**6.**  $1 \times 1\frac{2}{3} = \frac{5}{6}$  **7.**  $1\frac{1}{4} = 2\frac{1}{2}$ 

The unknown factor is \_\_\_\_\_1.

The unknown factor is \_\_\_\_\_1.

**8.** Kadeem is making two drawings of an oak leaf. The dimensions of the first drawing will be  $\frac{1}{3}$  the dimensions of the leaf. The dimensions of the second drawing will be  $2\frac{1}{2}$  the dimensions of the leaf. If the length of the oak leaf is  $5\frac{1}{2}$  inches, will the length of each drawing be equal to, greater than, or less than  $5\frac{1}{2}$  inches?

# Problem Solving · Applications Real

9. MTR Penny wants to make a model of a beetle that is larger than life-size. Penny says she is going to use a scale factor of  $\frac{7}{12}$ . Does this make sense? Explain.

- **10.** Shannon, Mary, and John earn a weekly allowance. Shannon earns an amount that is  $\frac{2}{3}$  of what John earns. Mary earns an amount that is  $1\frac{2}{3}$  of what John earns. John earns \$20 a week. Who earns the greatest allowance? Who earns the least?
- **11.** Stuart rode his bicycle  $6\frac{3}{5}$  miles on Friday. On Saturday, he rode  $1\frac{1}{3}$  times as far as he rode on Friday. On Sunday, he rode  $\frac{5}{6}$  times as far as he rode on Friday. For 11a–11d, select True or False for each statement.
  - 11a. Stuart rode more miles on Saturday than he rode on Friday. ○ True ○ False
  - 11b. Stuart rode more miles on Friday than he rode on Saturday and Sunday combined.
    - True ○ False
  - 11c. Stuart rode fewer miles on Sunday than he rode on Friday.
    - True ○ False
  - 11d. Stuart rode more miles on Sunday than he rode on Saturday.

○ True ○ False





Complete the statement with equal to, greater than, or less than. **1.**  $\frac{2}{3} \times 1\frac{5}{8}$  will be \_\_\_\_\_\_ 1 $\frac{5}{8}$ . **2.**  $\frac{5}{5} \times 2\frac{3}{4}$  will be \_\_\_\_\_\_  $2\frac{3}{4}$ . Think:  $1 \times 1\frac{5}{8}$  is  $1\frac{5}{8}$ . Since  $\frac{2}{3}$  is less than 1,  $\frac{2}{3} \times 1\frac{5}{8}$  will be less than  $1\frac{5}{8}$ . **3.**  $3 \times 3\frac{2}{7}$  will be \_\_\_\_\_\_  $3\frac{2}{7}$ . **4.**  $9 \times 1\frac{4}{5}$  will be \_\_\_\_\_\_  $1\frac{4}{5}$ . **5.**  $1\frac{7}{8} \times 2\frac{3}{8}$  will be \_\_\_\_\_\_  $2\frac{3}{8}$ . **6.**  $3\frac{4}{9} \times \frac{5}{9}$  will be \_\_\_\_\_\_  $3\frac{4}{9}$ . Problem Solving Real

- **Compare Relative Size of Products** to Mixed Number Factors
- 7. Karim is making a scale drawing of a doghouse. The dimensions of the drawing will be  $\frac{1}{8}$  of the dimensions of the actual doghouse. The height of the actual doghouse is  $36\frac{3}{4}$  inches. Will the dimensions of Karim's drawing be equal to, greater than, or less than the dimensions of the actual doghouse?
- **8.** Jorge has a recipe that calls for  $2\frac{1}{3}$  cups of flour. He plans to make  $1\frac{1}{2}$  times the recipe. Will the amount of flour Jorge needs be equal to, greater than, or less than the amount of flour his recipe calls for?

**LESSON 10.4** 

**Interactive Examples** 

**Go Online** 

Practice and Homework

**9. [WRITE** *Math* Explain how scaling a mixed number by  $\frac{1}{2}$  will affect the size of the number.

### **Lesson Check**

- **10.** Jenna skis  $2\frac{1}{3}$  miles down the mountain. Her instructor skis  $1\frac{1}{2}$  times as far. Does Jenna ski a lesser, greater, or the same distance as her instructor?
- **11.** Suppose you multiply a fraction less than 1 by the mixed number  $2\frac{3}{4}$ . Will the product be less than, greater than, or equal to  $2\frac{3}{4}$ ?

### **Spiral Review**

- **12.** Washington County is shaped like a rectangle. It measures 15 miles by 9 miles. What is the county's area?
- **13.** Lysha jogged 7.8 miles. Riley jogged 0.5 times as far. How far did Riley jog?

- **14.** One bread recipe calls for  $2\frac{1}{3}$  cups of flour. Another bread recipe calls for  $2\frac{1}{2}$  cups of flour. Tim has 5 cups of flour. If he makes both recipes, how much flour will he have left over?
- **15.** On Monday, it rained  $1\frac{1}{4}$  inches. On Tuesday, it rained  $\frac{3}{5}$  inch. How much more did it rain on Monday than on Tuesday?

# **Find Unknown Fractional Lengths**

**I Can** solve real-world problems involving fractional lengths.

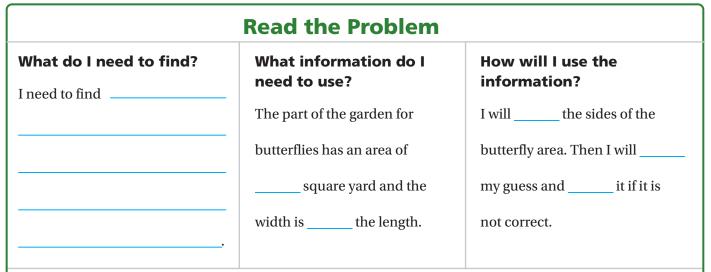
Florida's B.E.S.T.

**CHAPTER 10** 

- Fractions 5.FR.2.2, 5.FR.2.3
- Algebraic Reasoning 5.AR.1.2
- Geometric Reasoning 5.GR.2.1
- Mathematical Thinking & Reasoning MTR.1.1, MTR.2.1, MTR.4.1

# UNLOCK the Problem

Sori wants to design a rectangular garden with a section for flowers that attract butterflies. She wants the area of this section to be  $\frac{3}{4}$  square yard. If she wants the width to be  $\frac{1}{3}$  the length, what will the dimensions of the butterfly section be?



### **Solve the Problem**

I can try different lengths and calculate the widths by finding  $\frac{1}{3}$  of the length. For each length and width, I find the area and then compare. If the product is less than or greater than  $\frac{3}{4}$  square yard, I need to revise the length.

Guess		Check	Revise
Length (in yards)	Width (in yards) $(\frac{1}{3}$ of the length)	Area of Butterfly Garden (in square yards)	
$\frac{3}{4}$	$\frac{1}{3} \times \frac{3}{4} = \frac{1}{4}$	$\frac{3}{4} \times \frac{1}{4} = \frac{3}{16}$ too low	Try a longer length.
$2\frac{1}{4}$ , or $\frac{9}{4}$			

So, the dimensions of Sara's butterfly garden will be \_\_\_\_\_ yard by \_\_\_\_\_\_ yards.

### **Try Another Problem**

Marcus is building a rectangular box for his kitten to sleep in. He wants the area of the bottom of the box to be 360 square inches and the length of one side to be  $1\frac{3}{5}$  the length of the other side. What should the dimensions of the bottom of the bed be?



	<b>Read the Problem</b>	
What do I need to find?	What information do I need to use?	How will I use the information?
	Solve the Problem	
	the kitten's bed will be	
• MTR What if the longer side the shorter side was 20 inches l	was still $1\frac{3}{5}$ the length of the shorter song? What would the area of	ide and
the bettem of the bad be then?		

### Share and Show Moth Boord

1. When Pascal built a doghouse, he knew he wanted the floor of the house to have an area of 24 square feet. He also wanted the width to be  $\frac{2}{3}$  of the length. What are the dimensions of the doghouse?

First, choose two numbers that have a product of 24.

Guess: \_\_\_\_\_ feet and \_\_\_\_\_ feet

**Then,** check those numbers. Is the lesser number  $\frac{2}{3}$  of the other number?

Check:  $\frac{2}{3} \times \underline{\qquad} = \underline{\qquad}$ 

My guess is \_\_\_\_\_.

**Finally,** if the guess is not correct, revise it and check again. Continue until you find the correct answer.

So, the dimensions of the dog house are \_\_\_\_\_

- **2.** What if Pascal wanted the area of the floor to be 54 square feet and the width still to be  $\frac{2}{3}$  of the length? What would the dimensions of the floor be?
- ✓ 3. Leo wants to paint a mural that covers a wall with an area of 1,440 square feet. The height of the wall is  $\frac{2}{5}$  of its length. What is the length and the height of the wall?

### **On Your Own**

- **4.** Josue wants to make a drawing that is  $\frac{1}{4}$  the size of the original. If a tree in the original drawing is 14 inches tall and 5 inches wide, what will be the length and width of the tree in Josue's drawing?
- **5.** A blueprint is a scale drawing of a building. The dimensions of the blueprint for Patricia's dollhouse are  $\frac{1}{4}$  of the measurements of the actual dollhouse. The floor of the dollhouse has an area of 864 square inches. If the width of the dollhouse is  $\frac{2}{3}$  of the length, what are the dimensions of the floor on the blueprint of the doll house?
- 6. MTR Beth wants the floor of her tree house to be 48 square feet. She wants the length to be  $\frac{3}{4}$  the width. Using the strategy *guess, check, and revise,* Beth guesses the dimensions will be 4 feet by 12 feet. Is Beth's guess the correct dimensions? Explain.

- 7. Sally has a photograph that has an area of 35 square inches. She creates two enlargements of the photograph. The enlargements have areas of 140 square inches and 560 square inches. In each photograph, the length is  $1\frac{2}{5}$  times the width. Select which of the following could be the dimensions of the original photograph or one of the enlargements. Mark all that apply.
  - (A) 5 inches by 7 inches
  - **B** 20 inches by 28 inches
  - C 7 inches by 20 inches
  - **D** 21 inches by 15 inches
  - (E) 10 inches by 14 inches

# on the **Spot**

матн

### Show the Math

Demonstrate Your Thinking





### **Find Unknown Fractional Lengths**

Name

LESSON 10.5 Practice and Homework

Go Online Interactive Examples

1. Kamal's bedroom has an area of 120 square feet. The width of the room is  $\frac{5}{6}$  the length of the room. What are the dimensions of Kamal's bedroom?

Guess:  $6 \times 20 = 120$ Check:  $\frac{5}{6} \times 20 = 16\frac{2}{3}$ ; try a longer width. Guess:  $10 \times 12 = 120$ Check:  $\frac{5}{6} \times 12 = 10$ . Correct!

10 feet by 12 feet

**2.** Sezja is painting on a piece of canvas that has an area of 180 square inches. The length of the painting is  $1\frac{1}{4}$  times the width. What are the dimensions of the painting?

**3.** A small plane is flying a banner in the shape of a rectangle. The area of the banner is 144 square feet. The width of the banner is  $\frac{1}{4}$  the length of the banner. What are the dimensions of the banner?

**4. WRITE** *Math* Explain how you can use the strategy *guess, check, and revise* to solve problems that involve a given area when the relationship between the side lengths is also given.

### **Lesson Check**

- 5. Consuelo's living room is in the shape of a rectangle and has an area of 360 square feet. The width of the living room is  $\frac{5}{8}$  its length. What is the length of the living room?
- **6.** A rectangular park has an area of  $\frac{2}{3}$  square mile. The length of the park is  $2\frac{2}{3}$  the width of the park. What is the width of the park?

### **Spiral Review**

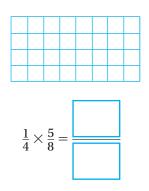
- 7. Olga babysits for  $3\frac{1}{2}$  hours on Friday and  $1\frac{1}{2}$  times as long on Saturday. Did Olga babysit more, fewer, or the same number of hours on Saturday than she did on Friday?
- **8.** Tory practiced basketball shots for  $\frac{2}{3}$  hour. Tim practiced basketball shots for  $\frac{3}{4}$  as much time as Tory did. How long did Tim practice basketball shots?

- **9.** Leah bought  $4\frac{1}{2}$  pounds of grapes. Of the grapes she bought,  $1\frac{7}{8}$  pounds were red grapes. The rest were green grapes. How many pounds of green grapes did Leah buy?
- **10.** To which place value is the following number rounded?

5.927 to 5.93

# **Chapter Review**





**2.** Diana worked on her science project for  $5\frac{1}{3}$  hours. Gabe worked on his science project  $1\frac{1}{4}$  times as long as Diana. Paula worked on her science project  $\frac{3}{4}$  times as long as Diana. For Problems 2a–2d, select True or False for each statement.

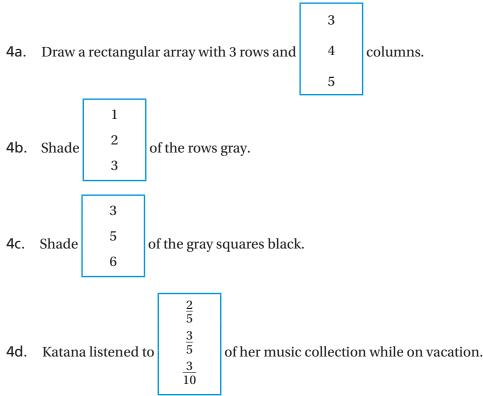
2a.	Diana worked longer on her science project than Gabe worked on his science project.	O True	○ False
2b.	Paula worked less on her science project than Diana worked on her science project.	• True	○ False
2c.	Gabe worked longer on his science project than Paula worked on her science project.	○ True	○ False
2d.	Gabe worked longer on his science project than Diana and Paula combined.	○ True	○ False

**3.** Luis wants to carpet the rectangular floor of his basement. The basement has an area of 864 square feet. The width of the basement is  $\frac{2}{3}$  its length. What is the length of the basement?

feet

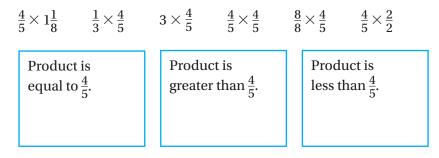


**4.** Katana put  $\frac{2}{3}$  of her music collection on her phone. While on vacation, she listened to  $\frac{3}{5}$  of the music on the player. How much of Katana's music collection did she listen to while on vacation? For Problems 4a-4d, choose the correct values to describe how to solve the problem.



- **5.** Logyn bought balloons. Four-fifths of the balloons are purple, and  $\frac{2}{3}$  of the purple balloons have stars on them. What fraction of the balloons are purple with stars on them? Show your work.
- **6.** Kayla walks  $\frac{17}{5}$  miles each day. Which of the following statements correctly describe how far she walks? Mark all that apply.
  - A Kayla walks  $\frac{20}{17}$  miles in 4 days.
  - **B** Kayla walks a little more than 10 miles in 3 days.
  - C Kayla walks 34 miles in 10 days.
  - D Kayla walks less than 6 miles in 6 days.

7. Write each multiplication expression in the correct box.



- 8. A postcard has an area of 24 square inches. Two enlargements of the postcard have areas of 54 square inches and 96 square inches. In each postcard, the length is  $1\frac{1}{2}$  times the width. Which of the following could be the dimensions of the postcard or one of the enlargements? Mark all that apply.
  - (A) 6 inches by 9 inches (D) 6 inches by 12 inches
  - **(B)** 10 inches by 15 inches (E) 4 inches by 6 inches
  - **C** 8 inches by 12 inches
- **9.** In a fifth grade class,  $\frac{4}{5}$  of the class has brown hair. Of the brown-haired classmates,  $\frac{3}{4}$  of them have long hair. Of the classmates with long brown hair,  $\frac{1}{3}$  of them have green eyes.

#### Part A

What fraction of the class has long brown hair?

\_\_\_\_\_ of the classmates

#### Part B

What fraction of the class has long brown hair and green eyes? Explain how you found your answer.

\_\_\_\_\_ of the classmates

- **10.** The length of a rectangle is  $5\frac{1}{4}$  yards. Give a possible width *w* for Problems 10a–10c.
  - 10a. For what width will the area of the rectangle be  $5\frac{1}{4}$  square yards?

W

5<u>1</u> yd

- 10b. For what width will the area of the rectangle be greater than  $5\frac{1}{4}$  square yards?
- **10c.** For what width will the area of the rectangle be less than  $5\frac{1}{4}$  square yards?
- **11.** Doreen lives  $\frac{3}{4}$  mile from the library. Sheila lives  $\frac{1}{3}$  as far away from the library as Doreen. For Problems 11a–11c, choose Yes or No to answer each question.

11a.	Does Doreen live farther from the library than Sheila?	○ Yes	O No
11b.	Does Sheila live $\frac{1}{4}$ mile from the library?	○ Yes	○ No
11c.	Does Sheila live twice as far from the library as Doreen?	○ Yes	O No

- **12.** Taniqua took a test where  $\frac{2}{3}$  of the questions were multiple choice. The rest of the questions were true/false. She got  $\frac{9}{10}$  of the multiple choice questions correct.
  - **12a**. What fraction of the test questions were multiple choice questions that she got correct?
  - 12b. If Taniqua got  $\frac{4}{5}$  of the true/false questions correct, what fraction of the test questions were true/false questions that she got incorrect?

Name

**13.** The table shows how many hours some of the part-time employees at a toy store worked last week.

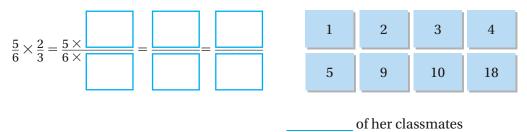
Name	Hours Worked
Conrad	6
Giovanni	9
Sally	11

This week, Conrad will work  $1\frac{3}{4}$  times as long as last week. Giovanni will work  $1\frac{1}{3}$  times as long as last week. Sally will work  $\frac{2}{3}$  the number of hours she worked last week. Match each employee's name to the number of hours he or she will work this week.

Employee	Hours This Week
Conrad •	• more than last week
Giovanni •	• fewer than last week
Sally •	

- **14.** Annika wants the floor of her chicken coop to be 48 square feet. She wants the length to be  $\frac{4}{3}$  of the width.
  - 14a. Estee designs a coop to be 12 feet by 4 feet. Does the design meet all of Annika's conditions? Explain.
  - 14b. What should the dimensions of the coop be?

**15.** Ruby conducted a survey and found that  $\frac{5}{6}$  of her classmates have a pet and  $\frac{2}{3}$  of those pets are dogs. What fraction of her classmates has dogs? Write a number from the number tiles in each box to complete the calculations shown below. You may use numbers more than once or not at all.



**16.** Revel is using the recipe below to make chicken noodle soup. She has enough chicken broth for  $\frac{3}{4}$  of a recipe.

#### Chicken Noodle Soup

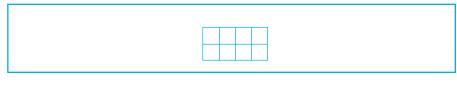
- 4 cups chicken broth
- 2 medium carrots, sliced
- 3 stalks of celery, sliced
- $\frac{1}{2}$  cup uncooked egg noodles
- $\frac{1}{8}$  teaspoon ground black pepper
- 1 cup shredded cooked chicken

#### Part A

Write an expression that Revel can use to determine how many cups of egg noodles she needs.

#### Part B

Draw a model to show how Revel can find the product from Part A.



#### Part C

Does Revel need more or less than  $\frac{1}{8}$  teaspoon of black pepper? How do you know?