

Chapter

9

# Add and Subtract Fractions and Mixed Numbers with Unlike Denominators

Shov	w What You Kno	w	
► Part of a W	hole Write a fraction to nam	e the shaded par	t.
1.	number of shaded parts number of total parts fraction	2.	number of shaded parts number of total parts fraction
Add and Su	ubtract Fractions Write the	sum or difference	е.
<b>3.</b> $\frac{2}{4} + \frac{1}{6} =$	<b>4.</b> $\frac{2}{5} + \frac{3}{10} =$	<b>5.</b> $\frac{7}{8} - \frac{3}{4} =$	<b>6.</b> $\frac{3}{4} - \frac{1}{6} =$
Multiples	Write the first six nonzero mu	ltiples.	
<b>7.</b> 6	<b>8.</b> 8		9. 4
MATH in the A Merchant Grain A a carpet beetle much longer is the beetle?	Beetle is about $\frac{1}{8}$ of an inch long. is about $\frac{1}{16}$ of an inch long. How e grain beetle than the carpet		

#### Visualize It

Use the  $\checkmark$  words to complete the H-diagram.



### Understand Vocabulary

#### **Complete each sentence.**

- 1. \_\_\_\_\_\_ are located at the same point on a number line.
- A number that has both a fraction and a whole number part is called a \_\_\_\_\_\_.
- **3.** When two fractions have the same number on the bottom, they are said to have a \_\_\_\_\_\_.



**Connect to Vocabulary** 



2. What other common denominator could you have used? \_\_\_\_\_\_

### **Examples**

**Subtract.**  $4\frac{5}{6} - 2\frac{3}{4}$ 

You can also use a common denominator to find the difference of mixed numbers with unlike denominators.

STEP 1	Estimate the difference.	$4\frac{5}{2}$
STEP 2	Find a common denominator. Use the common denominator to write equivalent fractions with like denominators.	$-2\frac{3}{4}$
STEP 3	Subtract the fractions. Subtract the whole numbers.	

**3. MTR** Explain how you know whether your answer is reasonable.

## Share and Show Math Board

**1.** Use a common denominator to write equivalent fractions with like denominators and then find the sum.

$$7\frac{2}{5} =$$
  
+  $4\frac{3}{4} = +$ 

Find the sum.

**2.**  $2\frac{3}{4} + 3\frac{3}{10}$  **3.**  $5\frac{3}{4} + 1\frac{1}{3}$ 

 $\checkmark$  **4.**  $3\frac{4}{5} + 2\frac{3}{10}$ 

=

#### Name

Find the difference.

**5.** 
$$9\frac{5}{6} - 2\frac{1}{3}$$
 **6.**  $10\frac{5}{9} - 9\frac{1}{6}$  **7.**  $7\frac{2}{3} - 3\frac{1}{6}$ 

On Your Own

Find the sum or difference.

**8.**  $1\frac{3}{10} + 2\frac{2}{5}$  **9.**  $8\frac{1}{6} + 7\frac{3}{8}$ 

Math Talk Engage in discussions on MTR Engage in discussions on mathematical thinking. Explain why you need to write equivalent fractions with common denominators to add  $4\frac{5}{6}$  and  $1\frac{1}{8}$ .

**10.**  $2\frac{1}{2} + 2\frac{1}{3}$ 

**11.** 
$$12\frac{3}{4} - 6\frac{1}{6}$$
 **12.**  $2\frac{5}{8} - 1\frac{1}{4}$  **13.**  $14\frac{7}{12} - 5\frac{1}{4}$ 

Find the sum or difference.

- 14.  $1\frac{5}{12} + 4\frac{1}{6}$  15.  $8\frac{1}{2} + 6\frac{3}{5}$  16.  $2\frac{1}{6} + 4\frac{5}{9}$  17.  $3\frac{5}{8} + \frac{5}{12}$  

   18.  $3\frac{2}{3} 1\frac{1}{6}$  19.  $5\frac{6}{7} 1\frac{2}{3}$  20.  $2\frac{7}{8} \frac{1}{2}$  21.  $4\frac{7}{12} 1\frac{2}{9}$
- **22.** Dakota makes a salad dressing by combining  $6\frac{1}{3}$  fluid ounces of oil and  $2\frac{3}{8}$  fluid ounces of vinegar in a jar. She then pours  $2\frac{1}{4}$  fluid ounces of the dressing onto her salad. How much dressing remains in the jar?
- **23.** This week, Talulla worked  $2\frac{1}{2}$  hours on Monday,  $2\frac{2}{3}$  hours on Tuesday, and  $3\frac{1}{4}$  hours on Wednesday. How many more hours will Talulla need to work this week to make her goal of  $10\frac{1}{2}$  hours a week?

## Problem Solving · Applications

#### Use the table to solve Problems 24 and 25.

- **24. MTR** Gavin plans to mix a batch of Tangerine paint. He expects to have a total of  $5\frac{3}{10}$  ounces of paint after he mixes the amounts of red and yellow. Explain how you can tell if Gavin's expectation is reasonable.
- Paint Gavin Uses<br/>(in ounces)RedYellowShade23342834283439233715556

**25.** Gavin mixes the amount of red from one shade of paint with the amount of yellow from a different shade of paint. He mixes the batch so he will have the greatest possible amount of paint. What amounts of red and yellow from which shades are used in the mixture? Explain your answer.



**26.** Martin won first place in the 100-meter dash with a time of  $14\frac{23}{100}$  seconds. Samuel came in second place with a time of  $15\frac{7}{10}$  seconds. For 26a–26d, select True or False for each statement.

26a.	A common denominator of the mixed numbers is 100.	⊖ True	⊖ False
26b.	To find the difference between the runners' times, Samuel's time needs to be rewritten.	⊖ True	⊖ False
26c.	Samuel's time written with a denominator of 100 is $15\frac{70}{100}$ .	⊖ True	○ False
26d.	Martin beat Samuel by $\frac{21}{25}$ second.	<mark>○</mark> True	<mark>○</mark> False

<b>1.</b> $3\frac{1}{2} - 1\frac{1}{5}$	<b>2.</b> $2\frac{1}{3} + 1\frac{5}{4}$	<b>3.</b> $4\frac{1}{8} + 2\frac{1}{3}$	<b>4.</b> $5\frac{1}{3} + 6\frac{1}{6}$
$3\frac{1}{2} \rightarrow 3\frac{5}{10}$			
$-1\frac{1}{5}$ $\rightarrow$ $-1\frac{2}{10}$			
2 <u>3</u> 10			
1 0	17 0	2 5	2 1
<b>5.</b> $2\frac{1}{4} + 1\frac{2}{5}$	<b>6.</b> $5\frac{17}{18} - 2\frac{2}{3}$	<b>7.</b> $6\frac{5}{4} - 1\frac{5}{8}$	<b>8.</b> $5\frac{3}{7} - 2\frac{1}{5}$

## Problem Solving

- **9.** Jacobi bought  $7\frac{1}{2}$  pounds of meatballs. He decided to cook  $1\frac{1}{4}$  pounds and freeze the rest. How many pounds did he freeze?
- **10.** Ms. Roth walked  $8\frac{1}{8}$  miles to a park and then  $7\frac{2}{5}$  miles home. How many miles did she walk?
- **11. WRITE** *Math* Write your own story problem using mixed numbers. Show the solution.

### **Lesson Check**

- **12.** Mrs. Rhein has a goal to jog  $4\frac{1}{2}$  miles each day. On Monday she jogged  $5\frac{9}{16}$  miles. By how much did she exceed her goal for that day?
- **13.** At the deli, Ricardo ordered  $3\frac{1}{5}$  pounds of cheddar cheese and  $2\frac{3}{4}$  pounds of mozzarella cheese. How many pounds of cheese did he order all together?

### **Spiral Review**

- **14.** The theater has 175 seats. There are 7 seats in each row. How many rows are there?
- **15.** During the first 14 days, 2,744 people visited a new store. The same number of people visited the store each day. About how many people visited the store each day?

- **16.** What number is 100 times as great as 0.3?
- **17.** Mark said that the product of 0.02 and 0.7 is 14. Mark is wrong. What is the product?

#### Name

### **Rename Mixed Numbers to Subtract**

**I Can** use renaming to find the difference of two mixed numbers.

G

## UNLOCK the Problem Real World

To practice for a race, Kara is running  $2\frac{1}{2}$  miles. When she reaches the end of her street, she knows that she has already run  $1\frac{5}{6}$  miles. How many miles does Kara have left to run? • Underline the sentence that tells you what you need to find.

Florida's B.E.S.T.

Fractions 5.FR.2.1

Algebraic Reasoning 5.AR.1.2

 Mathematical Thinking & Reasoning MTR.1.1, MTR.2.1, MTR.3.1

**CHAPTER 9** 

Lesson 2

• What operation should you use to solve the problem?

 $2\frac{1}{2} = 2\frac{6}{12} =$ 

 $-1\frac{5}{6} = -1\frac{10}{12} = -1\frac{10}{12}$ 



**Subtract.**  $2\frac{1}{2} - 1\frac{5}{6}$ 

- **STEP 1** Estimate the difference.
- **STEP 2** Find a common denominator. Use the common denominator to write equivalent fractions with like denominators.
- **STEP 3** Since  $\frac{6}{12}$  is less than  $\frac{10}{12}$ , rename  $2\frac{6}{12}$  as a mixed number with a fraction greater than 1.

**Think:**  $2\frac{6}{12} = 1 + 1 + \frac{6}{12} = 1 + \frac{12}{12} + \frac{6}{12} = 1\frac{18}{12}$ 

$$2\frac{6}{12} =$$

**STEP 4** Find the difference of the fractions. Then find the difference of the whole numbers. Check to make sure your answer is reasonable.

So, Kara has \_\_\_\_\_ mile left to run.

• **MTR** Explain why it is important to write equivalent fractions before renaming.



## On Your Own

#### Estimate. Then find the difference.

3. Estimate:	<b>4.</b> Estima	ate:	5. Estimate:	
$3\frac{2}{3} - 1\frac{11}{12}$	$4\frac{1}{4} - 2\frac{1}{3}$		$5\frac{2}{5} - 1\frac{1}{2}$	
Find the difference.				
<b>6.</b> $11\frac{1}{9} - 3\frac{2}{3}$	<b>7.</b> $6-3\frac{1}{2}$	<b>8.</b> $4\frac{3}{8} - 3\frac{1}{2}$	<b>9.</b> $9\frac{1}{6} - 3\frac{5}{8}$	
<b>10.</b> $1\frac{1}{5}-\frac{1}{2}$	<b>11.</b> $13\frac{1}{6} - 3\frac{4}{5}$	<b>12.</b> $12\frac{2}{5} - 5\frac{3}{4}$	<b>13.</b> $7\frac{3}{8} - 2\frac{7}{9}$	

**14.** Three commercials are played in a row between songs on the radio. The three commercials fill exactly 3 minutes of time. If the first commercial uses  $1\frac{1}{6}$  minutes, and the second uses  $\frac{3}{5}$  minute, how long is the third commercial?

•  $1\frac{17}{30}$  hours

•  $1\frac{9}{10}$  hours

•  $1\frac{11}{12}$  hours

**15.** Four students made videos for an art project. The table shows the length of each video.

Match each pair of videos with the correct difference between their times.

- Video 1 and Video 3 •
- Video 2 and Video 3 •
- Video 2 and Video 4

Art in Nature				
Video Time (in hours)				
1	$4\frac{3}{4}$			
2	4 <u>2</u> 5			
3	2 <u>5</u> 6			
4	2 <u>1</u> 2			

#### **Connect to Reading**

#### Summarize

An amusement park in Sandusky, Ohio, offers 17 amazing roller coasters for visitors to ride. One of the roller coasters runs at 60 miles per hour and has 3,900 feet of twisting track. This coaster also has 3 trains with 8 rows per train. Riders stand in rows of 4, for a total of 32 riders per train.

The operators of the coaster recorded the number of riders on each train during a run. On the first train, the operators reported that  $7\frac{1}{4}$  rows were filled. On the second train, all 8 rows were filled, and on the third train,  $5\frac{1}{2}$  rows were filled. How many more rows were filled on the first train than on the third train?

When you *summarize*, you restate the most important information in a shortened form to more easily understand what you have read.

**16. MTR** Identify and summarize the important information given in the problem.



#### Use the summary from Problem 16 to solve.

- **17.** Solve the problem.
- **18.** How many rows were empty on the first train? How many additional riders would it take to fill the empty rows? Explain your answer.



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## Problem Solving Real

- 7. Carlene bought  $8\frac{1}{16}$  yards of ribbon to decorate a shirt. She only used  $5\frac{1}{2}$  yards. How much ribbon does she have left over?
- 8. During his first vet visit, Pedro's puppy weighed  $6\frac{1}{8}$  pounds. On his second visit, he weighed  $9\frac{1}{16}$  pounds. How much weight did he gain between visits?
- **9. WRITE** *Math* Write a subtraction problem that has mixed numbers and requires renaming. Draw a visual model illustrating the steps you take to solve the problem.

### **Lesson Check**

- **10.** Natalia picked  $7\frac{1}{6}$  bushels of apples today and  $4\frac{5}{8}$  bushels yesterday. How many more bushels did she pick today?
- **11.** Max needs  $10\frac{1}{4}$  cups of flour to make a batch of pizza dough for the pizzeria. He only has  $4\frac{1}{2}$  cups of flour. How much more flour does he need to make the dough?

### **Spiral Review**

- **12.** The accountant charged \$35 for the first hour of work and \$23 for each hour after that. He earned a total of \$127. How many hours did he work?
- **13.** The soccer league needs to transport all 133 players to the tournament. If 4 players can ride in one car, how many cars are needed?

- **14.** What is five hundred million, one hundred fifteen written in standard form?
- **15.** Find the quotient.

 $6.39\div0.3$ 

## Describe and Create Fraction Patterns

**I Can** use addition and subtraction to describe a pattern or create a sequence with fractions.

E

## UNLOCK the Problem Real

Mr. Patrick wants to develop a new chili recipe for his restaurant. Each batch he makes uses a different amount of chili powder. The first batch uses  $3\frac{1}{2}$  ounces, the second batch uses  $4\frac{5}{6}$  ounces, the third uses  $6\frac{1}{6}$  ounces, and the fourth uses  $7\frac{1}{2}$  ounces. If this pattern continues, how much chili powder will he use in the sixth batch?

You can find the pattern in a sequence by comparing one term with the next term.

**STEP 1** Write the terms in the sequence as equivalent fractions with a common denominator. Then examine the sequence and compare the consecutive terms to find the rule used to make the sequence of fractions.



**STEP 2** Write a rule that describes the pattern in the sequence.

• Is the sequence increasing or decreasing from one term to the next? Explain.

Rule:



 $3\frac{1}{2}, 4\frac{5}{6}, 6\frac{1}{6}, 7\frac{1}{2},$ 

So, Mr. Patrick will use \_\_\_\_\_ ounces of chili powder in the sixth batch.

Florida's B.E.S.T.
Fractions 5.FR.2.1
Algebraic Reasoning 5.AR.3.1
Mathematical Thinking & Reasoning MTR.1.1, MTR.2.1, MTR.3.1

**CHAPTER 9** 

Lesson 3



<b>Examples</b> Find the unknown terms in the sequence.	
$1\frac{3}{4}, 1\frac{9}{16}, 1\frac{3}{8}, 1\frac{3}{16}, \_$ ,,,, $\frac{7}{16}, \frac{1}{4}$	
<b>STEP 1</b> Write the terms in the sequence as equivalent fractions with a common denominator.	
,, _,, _	
<b>STEP 2</b> Write a rule describing the pattern in the sequence.	
<ul> <li>What operation can be used to describe a sequence that increases?</li> </ul>	
• What operation can be used to describe a sequence that decreases?	
Rule:	
STEP 3 Use your rule to find the unknown terms. Then	MTR Engage in discussions on 4.1 mathematical thinking.
complete the sequence.	How do you know whether your rule for a sequence would involve addition or subtraction?
Try This!	
A Write a rule for the sequence. Then find the unknown term.	
$1\frac{1}{12}, \frac{5}{6}, \_, \frac{1}{3}, \frac{1}{12}$	
Rule:	

**B** Write the first four terms of the sequence.

**Rule:** start at  $\frac{1}{4}$ , add  $\frac{3}{8}$ 

Share and Show Math Board	
Vrite a rule for the sequence.	
<b>1.</b> $\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, \ldots$	$\checkmark$ <b>2.</b> $\frac{1}{9}, \frac{1}{3}, \frac{5}{9}, \ldots$
Think: Is the sequence increasing or decreasing?	?
Rule:	Rule:
rite a rule for the sequence. Then find the u	nknown term.
<b>3.</b> $\frac{3}{10}, \frac{2}{5}, $ , $\frac{3}{5}, \frac{7}{10}$	$\checkmark$ <b>4.</b> $10\frac{2}{3}$ , $9\frac{11}{18}$ , $8\frac{5}{9}$ ,, , $6\frac{1}{3}$
Rule:	Rule:
Write the first four terms of the sequence.	
<b>5.</b> Rule: start at $5\frac{3}{4}$ , subtract $\frac{5}{8}$	<b>6.</b> Rule: start at $\frac{3}{8}$ , add $\frac{3}{16}$
· / / / /	,,,,
<b>7.</b> Rule: start at $2\frac{1}{3}$ , add $2\frac{1}{4}$	<b>8.</b> Rule: start at $\frac{8}{9}$ , subtract $\frac{1}{18}$

**10.** Mr. Kuri drove  $78\frac{1}{3}$  miles on Monday,  $77\frac{1}{12}$  miles on Tuesday, and  $75\frac{5}{6}$  miles on Wednesday. If he continues this pattern on Thursday and Friday, how many fewer miles will he drive on Friday than on Tuesday?

## Problem Solving · Applications Real

- **11.** When Bill bought a marigold plant, it was  $\frac{1}{4}$  inch tall. After the first week, it measured  $1\frac{1}{12}$  inches tall. After the second week, it was  $1\frac{11}{12}$  inches. After week 3, it was  $2\frac{3}{4}$  inches tall. Assuming the growth of the plant was constant, what was the height of the plant at the end of week 4?
- **12.** What if Bill's plant grew at the same rate but was  $1\frac{1}{2}$  inches when he bought it? How tall would the plant be after 3 weeks?
- MATH on the Spot



**13.** Kendra hiked each day for a week. The first day she hiked  $\frac{1}{8}$  mile, the second day she hiked  $\frac{3}{8}$  mile, and the third day she hiked  $\frac{5}{8}$  mile.

What is the rule for the distance Kendra hikes each day? Show how you can check your answer.

If the pattern continues, how many miles will Kendra hike on day 7? Explain how you found your answer.

## **Describe and Create Fraction Patterns**

Go Online

**Practice and Homework** 

Interactive Examples

**LESSON 9.3** 

Write a rule for the sequence. Then, find the unknown term.

**1.** 
$$\frac{1}{2}, \frac{2}{3}, \frac{5}{6}, 1, 1, 1\frac{1}{6}$$

Name

**2.**  $1\frac{3}{8}$ ,  $1\frac{3}{4}$ ,  $2\frac{1}{8}$ , ,  $2\frac{7}{8}$ 

Think: The pattern is increasing. Add  $\frac{1}{6}$  to find the next term.

Rule: \_\_\_\_\_

**3.**  $1\frac{9}{10}, 1\frac{7}{10}, \_$ ,  $1\frac{3}{10}, 1\frac{1}{10}$ 

Rule:

#### Write the first four terms of the sequence.

**5.** Rule: start at  $\frac{1}{2}$ , add  $\frac{1}{3}$ 

Rule:

**4.**  $2\frac{5}{12}, 2\frac{1}{6}, 1\frac{11}{12}, \dots, 1\frac{5}{12}$ 

Rule: \_\_\_\_\_

**6.** Rule: start at  $3\frac{1}{8}$ , subtract  $\frac{3}{4}$ 

## Problem Solving Real

- 7. Jarett's puppy weighed  $3\frac{3}{4}$  ounces at birth. At one week old, the puppy weighed  $5\frac{1}{8}$  ounces. At two weeks old, the puppy weighed  $6\frac{1}{2}$  ounces. If the weight gain continues in this pattern, how much will the puppy weigh at three weeks old?
- **8.** A baker started out with 12 cups of flour. She had  $9\frac{1}{4}$  cups of flour left after the first batch of batter she made. She had  $6\frac{1}{2}$  cups of flour left after the second batch of batter she made. If she makes two more batches of batter, how many cups of flour will be left?
- **9. WRITE** *Math* Make up your own sequence of 5 fractions or mixed numbers. Offer the sequence to another student to try to find the next fraction in the sequence.

### **Lesson Check**

**10.** What is a rule for the sequence?

**11.** Jaime biked  $5\frac{1}{4}$  miles on Monday,  $6\frac{7}{8}$  miles on Tuesday, and  $8\frac{1}{2}$  miles on Wednesday. If he continues the pattern, how many miles will he bike on Friday?

$$\frac{5}{6}$$
,  $1\frac{1}{2}$ ,  $2\frac{1}{6}$ ,  $2\frac{5}{6}$ , . .

### **Spiral Review**

- **12.** Jaylyn rode her bicycle in a bike-a-thon. She rode 33.48 miles in 2.7 hours. If she rode at the same speed, what was her speed in miles per hour?
- **13.** One week a company filled 546 boxes with widgets. Each box held 38 widgets. How many widgets did the company pack in boxes that week?

- **14.** Write an expression that represents the statement "Add 9 and 3, then multiply by 6."
- 15. Mason took 9.4 minutes to complete the first challenge in the Champs Challenge. He completed the second challenge2.65 minutes faster than the first challenge. How long did it take Mason to complete the second challenge?

#### Name

## **Apply Properties of Addition**

# **I Can** use properties to help add fractions with unlike denominators.

**CONNECT** You can use properties of addition to help you add fractions with unlike denominators.

Commutative Property:  $\frac{1}{2} + \frac{3}{5} = \frac{3}{5} + \frac{1}{2}$ Associative Property:  $\left(\frac{2}{9} + \frac{1}{8}\right) + \frac{3}{8} = \frac{2}{9} + \left(\frac{1}{8} + \frac{3}{8}\right)$ 



Florida's B.E.S.T. • Fractions 5.FR.2.1

**CHAPTER 9** 

Lesson **4** 

- Algebraic Reasoning 5.AR.1.2
- Mathematical Thinking & Reasoning MTR.1.1, MTR.2.1, MTR.3.1, MTR.4.1, MTR.6.1

#### Remember

Parentheses () tell which operation to do first.

2

## UNLOCK the Problem Real World

Jane and her family are driving to Big Lagoon State Park. On the first day, they travel  $\frac{1}{3}$  of the total distance. On the second day, they travel  $\frac{1}{3}$  of the total distance in the morning and then  $\frac{1}{6}$  of the total distance in the afternoon. How much of the total distance has Jane's family driven by the end of the second day?

#### Use the Associative Property.

 $\frac{1}{3} + \left(\frac{1}{3} + \frac{1}{6}\right) = \left(\begin{array}{c} + \end{array}\right) +$ 

So, Jane's family has driven \_\_\_\_\_ of the total distance by

Day 1 + Day 2



Write equivalent fractions with like denominators. Then add.



MTR Engage in discussions on 4.1 mathematical thinking.

Explain why grouping the fractions differently makes it easier to find the sum.



the end of the second day.

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Use the Commutative Property to put fractions with like denominators next to each other.

Use the Associative Property to group fractions with like denominators together.

Use mental math to add the fractions with like denominators.

Write equivalent fractions with like denominators. Then add.

Rename and simplify.

#### Try This! Use properties to solve. Show each step and name the property used.

=

=

+



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## Share and Show Math Board

Use the properties and mental math to solve.

**1.** 
$$\left(2\frac{5}{8}+\frac{5}{6}\right)+1\frac{1}{8}$$
  $(2\frac{5}{12}+\frac{5}{12}+\frac{3}{4})$ 

$$\checkmark$$
 **3.**  $\left(3\frac{1}{4} + 2\frac{5}{6}\right) + 1\frac{3}{4}$ 



## On Your Own

Use the properties and mental math to solve.

**4.**  $\left(\frac{2}{7} + \frac{1}{3}\right) + \frac{2}{3}$  **5.**  $\left(\frac{1}{5} + \frac{1}{2}\right) + \frac{2}{5}$  **6.**  $\left(\frac{1}{6} + \frac{3}{7}\right) + \frac{2}{7}$ 

**7.** 
$$\left(2\frac{5}{12}+4\frac{1}{4}\right)+\frac{1}{4}$$
 **8.**  $1\frac{1}{8}+\left(5\frac{1}{2}+2\frac{3}{8}\right)$  **9.**  $\frac{5}{9}+\left(\frac{1}{9}+\frac{4}{5}\right)$ 

**10.** Tina used  $10\frac{1}{2}$  yards of yarn to make three yarn dolls. She used  $4\frac{1}{2}$  yards of yarn for the first doll and  $2\frac{1}{5}$  yards for the second doll. How much yarn did Tina use for the third doll?

## Problem Solving · Applications

#### Use the map to solve Problems 11 and 12.

- **11.** Jules rides a bike from the sports complex to the school. Then Jules rides from the school to the mall, and then on to the library. Kyle rides his bike from his house to the mall, and then to the library. Who rides farther? How many miles farther?
- 12. On one afternoon, Mario walks from his house to the library. That evening, Mario walks from the library to the mall, and then to Kyle's house. Describe how you can use the properties to find how far Mario walks.





- **13.** MTR Kyle is adding the distances between the school and the mall, the mall and the park, and the mall and his house. He writes  $\frac{2}{5} + \frac{2}{3} + \frac{4}{5}$ . Rewrite Kyle's expression using properties so the fractions are easier to add.
- **14.** For 14a–14c, tell whether the Commutative Property or the Associative Property can be used to show that each equation is true without calculating. Choose the correct property of addition.

14a.
 
$$\frac{9}{10} + (\frac{3}{10} + \frac{5}{6}) = (\frac{9}{10} + \frac{3}{10}) + \frac{5}{6}$$
 Associative Property  
Commutative Property

 14b.
  $(\frac{3}{4} + \frac{1}{5}) + \frac{1}{4} = (\frac{1}{5} + \frac{3}{4}) + \frac{1}{4}$ 
 Associative Property  
Commutative Property

 14c.
  $(3\frac{1}{2} + 2\frac{1}{8}) + 1\frac{5}{8} = 3\frac{1}{2} + (2\frac{1}{8} + 1\frac{5}{8})$ 
 Associative Property  
Commutative Property

## **Apply Properties of Addition**

Use the properties and mental math to solve.

1. 
$$\left(2\frac{1}{3}+1\frac{2}{5}\right)+3\frac{2}{3}$$
  
 $=\left(1\frac{2}{5}+2\frac{1}{3}\right)+3\frac{2}{3}$   
 $=1\frac{2}{5}+\left(2\frac{1}{3}+3\frac{2}{3}\right)$   
 $=1\frac{2}{5}+6$   
 $=7\frac{2}{5}$   
2.  $8\frac{1}{5}+\left(4\frac{2}{5}+3\frac{3}{10}\right)$   
 $=1\frac{2}{5}+6$   
 $=7\frac{2}{5}$   
4.  $2\frac{1}{10}+\left(1\frac{2}{7}+4\frac{9}{10}\right)$   
5.  $3\frac{1}{4}+\left(3\frac{1}{4}+5\frac{1}{5}\right)$   
6.  $1\frac{1}{4}+\left(3\frac{2}{3}+5\frac{3}{4}\right)$ 

## Problem Solving Real

- **7.** Eliza rode her bike  $6\frac{1}{2}$  miles from her house to the library and then another  $2\frac{2}{5}$  miles to her friend Milo's house. If Carson's house is  $2\frac{1}{2}$  miles beyond Milo's house, how far would she travel from her house to Carson's house?
- 8. Hassan made a vegetable salad with  $2\frac{3}{8}$  pounds of tomatoes,  $1\frac{1}{4}$  pounds of asparagus, and  $2\frac{7}{8}$  pounds of potatoes. How many pounds of vegetables did he use altogether?
- **9. WRITE** *Math* Write the definitions for the Commutative Property and Associative Property. Give an example for each property.

Go Online	
Interactive Examples	s

### **Lesson Check**

**10.** What is the sum of  $2\frac{1}{3}$ ,  $3\frac{5}{6}$ , and  $6\frac{2}{3}$ ?

**11.** Letitia has  $7\frac{1}{6}$  yards of yellow ribbon,  $5\frac{1}{4}$  yards of orange ribbon, and  $5\frac{1}{6}$  yards of brown ribbon. How much ribbon does she have altogether?

### **Spiral Review**

- **12.** Juanita wrote  $3 \times 47$  as  $3 \times 40 + 3 \times 7$ . What property did she use to rewrite the expression?
- **13.** What is the value of the expression?

 $18 - 2 \times (4 + 3)$ 

- **14.** Evan spent \$15.89 on 7 pounds of birdseed. How much did the birdseed cost per pound?
- **15.** Cade rode  $1\frac{3}{5}$  miles on Saturday and  $1\frac{3}{4}$  miles on Sunday. How far did he ride on the two days?

## Practice Addition and Subtraction Using Equations



**CHAPTER 9** 

**(I Can)** use the strategy *work backward* to help solve a problem with fractions that involves addition and subtraction.



## UNLOCK the Problem Real

The Diaz family is cross-country skiing the Big Tree trails, which have a total length of 4 miles. Yesterday, they skied the  $\frac{7}{10}$ -mile Oak Trail. Today, they skied the  $\frac{3}{5}$ -mile Pine Trail. If they plan to ski all the Big Tree trails, how many more miles do they have left to ski?



Use the graphic organizer to help you solve the problem.

Read the Problem					
What do I need to find?	What information do I need to use?	How will I use the information?			
	I need to use the distance	I can work backward by starting with the			
	and the total distance	and each distance they have already skied to find the distance they have left.			
Addition and subtraction are invers using the same numbers, one opera	<b>Solve the Problem</b> se operations. By working backward and ation undoes the other.	d			
• Write an equation.	• Then wor	k backward to find <i>m</i> .			
miles skied $+$ miles skied $+$ today $+$	miles they total need to ski = distance $\psi$ $\psi$	= m			
++	<i>m</i> = 4	= <i>m</i>			
So, the family has mi	iles left to ski.				

• **MTR** Explain how you know your answer is reasonable.

## Try Another Problem

As part of their study of Native American basket weaving, Lia's class is making wicker baskets. Lia starts with a strip of wicker 36 inches long. From the strip, she first cuts one piece but does not know its length, and then cuts a piece that is  $6\frac{1}{2}$  inches long. The piece left is  $7\frac{3}{4}$  inches long. What is the length of the first piece she cut from the strip?



	Read the Problem				
What do I need to find?	What information do I need to use?	How will I use the information?			
	Solve the Problem				
So, the length of the first piece cut wa	sinches.	MTR Demonstrate understanding			

What other strategy could you use to solve the problem?

#### Share and Show Math Board

**(1.** Caitlin has  $4\frac{3}{4}$  pounds of clay. She uses  $1\frac{1}{10}$  pounds to make a cup, and another 2 pounds to make a jar. How many pounds are left?

> First, write an equation to model the problem.

Next, work backward and rewrite the equation to find *x*.

Solve.

pounds of clay remain. So,

- 2. What if Caitlin had used more than 2 pounds of clay to make a jar? Would the amount remaining have been more or less than your answer to Problem 1?
- **3.** A pet store donated 50 pounds of food for adult dogs, puppies, and cats to an animal shelter.  $19\frac{3}{4}$  pounds was adult dog food and  $18\frac{7}{8}$  pounds was puppy food. How many pounds of cat food did the pet store donate?

### **Unlock the Problem**

- $\sqrt{}$  Plan your solution by deciding on the steps you will use.
- $\sqrt{}$  Check your exact answer by comparing it with your estimate.
- ✓ Check your answer for reasonableness.

#### Show the Math

Demonstrate Your Thinking

**4.** Thelma spent  $\frac{1}{6}$  of her weekly allowance on dog toys,  $\frac{1}{4}$  on a dog collar, and  $\frac{1}{3}$  on dog food. What fraction of her weekly allowance is left?

### On Your Own

- **5.** Adriel is making a model of a Native American canoe. He has  $5\frac{1}{2}$  feet of wood. He uses  $2\frac{3}{4}$  feet for the hull and  $1\frac{1}{4}$  feet for a paddle. How much wood does he have left?
- **6.** Beth's summer vacation lasted 87 days. At the beginning of her vacation, she spent some time at soccer camp, 5 days at her grandmother's house, and 13 days visiting Glacier National Park with her parents. She then had 48 vacation days remaining. How many weeks did Beth spend at soccer camp?



**7. MTR** You can buy 2 DVDs for the same price you would pay for 3 CDs selling for \$13.20 apiece. Explain how you could find the price of 1 DVD.

**8.** Julio caught 3 fish weighing a total of  $23\frac{1}{2}$  pounds. One fish weighed  $9\frac{5}{8}$  pounds and another weighed  $6\frac{1}{4}$  pounds. How much did the third fish weigh? Use the numbers and symbols to write an equation that represents the problem. Then solve the equation. Symbols may be used more than once or not at all.



weight of third fish: \_\_\_\_\_ pounds

## Practice Addition and Subtraction Using Equations

#### LESSON 9.5 Practice and Homework

Go Online Interactive Examples

#### Read each problem and solve.

**1.** From a board 8 feet in length, Emmet cut two  $2\frac{1}{3}$ -foot bookshelves. How much of the board remained?

Write an equation: 
$$\mathbf{8} = \mathbf{2}\frac{\mathbf{1}}{\mathbf{3}} + \mathbf{2}\frac{\mathbf{1}}{\mathbf{3}} + \mathbf{x}$$

Rewrite the equation to work backward:

$$8-2\frac{1}{3}-2\frac{1}{3}=x$$

Subtract twice to find the length remaining:  $3\frac{1}{3}$  feet

- **2.** Lynne bought a bag of grapefruit,  $1\frac{5}{8}$  pounds of apples, and  $2\frac{3}{16}$  pounds of bananas. The total weight of her purchases was  $7\frac{1}{2}$  pounds. How much did the bag of grapefruit weigh?
- **3.** Mattie's house consists of two stories and an attic. The first floor is  $8\frac{5}{6}$  feet tall, the second floor is  $8\frac{1}{2}$  feet tall, and the entire house is  $24\frac{1}{3}$  feet tall. How tall is the attic?
- **4.** It is  $10\frac{3}{5}$  miles from Alston to Barton and  $12\frac{1}{2}$  miles from Barton to Chester. The distance from Alston to Durbin, via Barton and Chester, is 35 miles. How far is it from Chester to Durbin?
- 5. Marcie bought a 50-foot roll of packing tape. She used two  $8\frac{5}{6}$ -foot lengths. How much tape is left on the roll?
- 6. **WRITE** Math Write a word problem involving fractions for which you would use the *work backward* strategy and addition to solve. Include your solution.

### **Lesson Check**

- **7.** Dardby spent  $\frac{3}{8}$  of her allowance on clothes and  $\frac{1}{6}$  on entertainment. What fraction of her allowance did she spend on other items?
- **8.** Cara bought a tree seedling that was  $2\frac{1}{4}$  feet tall. During the first year, it grew  $1\frac{1}{6}$  feet. After two years, it was 5 feet tall. How much did the seedling grow during the second year?

### **Spiral Review**

**9.** Solve for *n*.

 $394 \div n = 0.394$ 

**10.** What expression can be used for estimating  $868 \div 28$ ?

*n* =

- **11.** Justin gave the clerk \$20 to pay a bill of \$6.57. How much change should Justin get?
- **12.** What is the value of the following expression?

$$7 + 18 \div (6 \div 3)$$

## **Chapter Review**





**2.** Rodrigo practiced playing the guitar  $15\frac{1}{3}$  hours over the past 3 weeks. He practiced for  $6\frac{1}{4}$  hours during the first week and  $4\frac{2}{3}$  hours during the second week. How much time did Rodrigo spend practicing during the third week? Use the numbers and symbols to write an equation that represents the problem. Then solve the equation. Symbols may be used more than once or not at all.



Practice time during third week: \_\_\_\_\_ hours



- **3.** Liam bought  $5\frac{7}{8}$  pounds of steak. He used  $2\frac{1}{16}$  pounds of the steak for a cookout. For numbers 3a–3c, fill in each blank.
  - **3a**. Rounded to the closest benchmark, Liam bought about pounds of steak.
  - **3b.** Rounded to the closest benchmark, Liam used about pounds of steak for the cookout.
  - **3c.** Liam has about pounds of steak remaining after the cookout.
- **4.** Jackson picked apples for his family. He picked a total of  $6\frac{1}{2}$  pounds. He took  $2\frac{3}{4}$  pounds to his aunt and  $1\frac{5}{8}$  pounds to his mother. How many pounds of apples were left to give to his grandmother? Use the numbers and symbols to write an equation that represents the problem, then solve the equation. Symbols may be used more than once or not at all.

6 <u>1</u>	$2\frac{3}{4}$	1 <u>5</u>	x	=	+	

Weight of apples Jackson gave to his grandmother: \_\_\_\_\_ pounds

**5.** Write  $4\frac{3}{5}$  and  $3\frac{2}{4}$  using a common denominator.



**6.** Jill brought  $2\frac{1}{3}$  boxes of carrot muffins for a bake sale. Mike brought  $1\frac{3}{4}$  boxes of apple muffins. What is the total number of boxes of muffins Jill and Mike brought to the bake sale?

boxes of muffins

#### Name

- 7. Caymen bought  $1\frac{7}{8}$  pounds of ham and  $2\frac{1}{4}$  pounds of turkey to make sandwiches for a picnic. He uses  $2\frac{1}{3}$  pounds of meat on the sandwiches. How many pounds of meat are left?
  - **7a**. Write an equation to model the problem. Let *x* be the number of pounds of meat that are left.



7b. Work backwards to find *x*.



7c. Answer the question.



**8.** For numbers 8a–8c, tell whether the Commutative Property or the Associative Property can be used to show each equation is true without calculating. Choose the correct property of addition.

8a. 
$$\frac{1}{6} + \left(\frac{7}{8} + \frac{5}{6}\right) = \frac{1}{6} + \left(\frac{5}{6} + \frac{7}{8}\right)$$
Associative Property  
Commutative Property8b.  $\left(\frac{7}{10} + \frac{1}{3}\right) + \frac{1}{10} = \left(\frac{1}{3} + \frac{7}{10}\right) + \frac{1}{10}$ Associative Property  
Commutative Property8c.  $\left(6\frac{2}{5} + \frac{4}{9}\right) + 3\frac{2}{9} = 6\frac{2}{5} + \left(\frac{4}{9} + 3\frac{2}{9}\right)$ Associative Property  
Commutative Property

9. Joshua uses a rule to write the following sequence of numbers.

 $\frac{1}{6}, \frac{1}{2}, \frac{5}{6}, \quad 1\frac{1}{2}$ What rule did Joshua use? **10.** Alexis has a puppy that weighed  $5\frac{3}{5}$  pounds when she got it. The puppy gained  $\frac{2}{10}$  pounds each week for 4 weeks. How much did the puppy weigh at the end of the fourth week?

\_\_\_ pounds

**11.** Mr. Cohen drives  $84\frac{2}{10}$  miles on Tuesday,  $84\frac{6}{10}$  miles on Wednesday, and 85 miles on Thursday.

#### Part A

What is the rule for the distance Mr. Cohen drives each day? Show how you can check your answer.

### Part B

If the pattern continues, how many miles will Mr. Cohen drive on Sunday? Explain how you found your answer. Name \_\_\_\_\_

**12.** Write a rule for the sequence. Then find the unknown term.

$$3\frac{7}{12}, 3\frac{1}{4},$$
\_\_\_\_\_\_,  $2\frac{7}{12}, 2\frac{1}{4}$ 

Rule:

**13.** Four students spent time volunteering last weekend. The table shows how much time each student spent volunteering.

Volunteering				
Student	Time (in hours)			
Amy	4 <u>5</u>			
Beth	6 <sup>1</sup> <sub>2</sub>			
Victor	5 <sup>3</sup> / <sub>4</sub>			
Cal	5 <del>2</del> 3			

Match each pair of students with the difference between how much time they spent volunteering.

Amy and Victor •	• $\frac{3}{4}$ hour
Cal and Beth •	• $\frac{11}{12}$ hour
Beth and Victor •	• $\frac{5}{6}$ hour

**14.** For 14a–14d, tell which expressions require you to rename mixed numbers before you can subtract. Find each difference. Write each expression and the difference as an equation in the correct box.

14a.	$2\frac{1}{3} - 1\frac{3}{4}$	14c	$5\frac{2}{3}-2\frac{5}{8}$
14b.	$1\frac{3}{4} - \frac{7}{8}$	14d	$.  6\frac{1}{5} - 2\frac{1}{3}$
	Requires Renaming		Does Not Require Renaming

- **15.** Mr. Clements painted his barn for  $3\frac{3}{5}$  hours in the morning. He painted the barn for  $5\frac{3}{4}$  hours in the afternoon. For numbers 15a–15c, select True or False for each statement.
  - 15a. A common denominator of the mixed numbers is 20.
    15b. The amount of time spent painting in the morning can be rewritten as 3<sup>15</sup>/<sub>20</sub> hours.
    15c. Mr. Clements spent 2<sup>3</sup>/<sub>20</sub> hours or True False longer painting in the afternoon than the morning.
- **16.** Guillermo practiced piano for  $2\frac{2}{3}$  hour during the week and  $1\frac{3}{4}$  hour on the weekend.

#### Part A

Complete the calculations below to write equivalent fractions with a common denominator.





#### Part B

How much time did Guillermo spend practicing piano in all? Explain how you found your answer.

### Part C

How much more time did he spend practicing during the week than on the weekend? Explain how you found your answer.