



Show What You Know

Check your understanding of important skills.

Name	
------	--

2-Digit Addition and Subtraction Find the sum or difference.



2.	Hundreds	Tens	Ones
		8	2
_		4	7

Decimals Greater Than One Write the word form and the expanded form for each.

3. 3.4

1.	2	.5	1

Relate Fractions and Decimals Write as a decimal or a fraction.

- **5.** 0.8
- **8.** $\frac{6}{10}$

9. 0.90

6. $\frac{5}{100}$

7. 0.46

10. $\frac{35}{100}$

MATH DETECTIVE WITH CARMEN SANDIEGO

Jason has 4 tiles. Each tile has a number printed on it. The numbers are 2, 3, 6, and 8. A decimal number is formed using the tiles and the clues. Be a Math Detective and find the number.

Clues

The digit in the tens place is the greatest number.
The digit in the tenths place is less than the digit in the hundredths place.

• The digit in the ones place is greater than the digit in the hundredths place.



Vocabulary Builder





Thousandths

Essential Question How can you describe the relationship between two decimal place-value positions?

Investigate

Materials color pencils straightedge

Thousandths are smaller parts than hundredths. If one hundredth is divided into ten equal parts, each part is one **thousandth**.

Use the model at the right to show tenths, hundredths, and thousandths.

- **A.** Divide the larger square into 10 equal columns or rectangles. Shade one rectangle. What part of the whole is the shaded rectangle? Write that part as a decimal and a fraction.
- **B.** Divide each rectangle into 10 equal squares. Use a second color to shade in one of the squares. What part of the whole is the shaded square? Write that part as a decimal and a fraction.
- **C.** Divide the enlarged hundredths square into 10 equal columns or rectangles. If each hundredths square is divided into ten equal rectangles, how many parts will the model have?

Use a third color to shade one rectangle of the enlarged hundredths square. What part of the whole is the shaded rectangle? Write that part as a decimal and a fraction.





MATHEMATICAL PRACTICES

Math Talk There are 10 times as many hundredths as there are tenths. Explain how the model shows this.

© Houghton Mifflin Harcourt Publishing Company

Draw Conclusions

1. Explain what each shaded part of your model in the Investigate section shows. What fraction can you write that relates each shaded

part to the next greater shaded part? _

2. Identify and describe a part of your model that shows one thousandth. Explain how you know.

Make Connections

The relationship of a digit in different place-value positions is the same with decimals as it is with whole numbers. You can use your understanding of place-value patterns and a place-value chart to write decimals that are 10 times as much as or $\frac{1}{10}$ of any given decimal.



Use the steps below to complete the table.

- STEP 1 Write the given decimal in a place-value chart.
- STEP 2 Use the place-value chart to write a decimal that is 10 times as much as the given decimal.
- STEP 3 Use the place-value chart to write a decimal that is $\frac{1}{10}$ of the given decimal.

Decimal	10 times as much as	1 10 of
0.03		
0.1		
0.07		

Math Talk Describe the pattern you see when you move one decimal place value to the right and one decimal place value to the left.

MATHEMATICAL PRACTICES

Name _ Share and Show MATH Write the decimal shown by the shaded parts of each model. 1. 2. **ਓ** 4. 3. Complete the sentence. **6.** 0.007 is $\frac{1}{10}$ of _____. **5.** 0.6 is 10 times as much as _____. **7.** 0.008 is $\frac{1}{10}$ of _____. **8.** 0.5 is 10 times as much as _____.

	Decimal	10 times as much as	10 of
9.	0.2		
10.	0.07		
11.	0.05		
12.	0.4		

C Houghton Mifflin Harcourt Publishing Company

Use place-value	patterns to	complete	the table.
doe place value	patterno to	complete	the table.

	Decimal	10 times as much as	$\frac{1}{10}$ of
13.	0.06		
14.	0.9		
15.	0.3		
16.	0.08		

Problem Solving REAL WORLD

Use the table for 17–20.

- **17.** What is the value of the digit 2 in the carpenter bee's length?
- If you made a model of a bumblebee that was 10 times as large as the actual bee, how long would the model be in meters? Write your answer as a decimal.
- The sweat bee's length is 6 thousandths of a meter. Complete the table by recording the sweat bee's length.
- **20.** An atlas beetle is about 0.14 of a meter long. How does the length of the atlas beetle compare to the length of a leafcutting bee?

21. Write Math Explain how you can use place value to describe how 0.05 and 0.005 compare.

- **22. Test Prep** What is the relationship between 1.0 and 0.1?
 - (\mathbf{A}) 0.1 is 10 times as much as 1.0
 - **B** 1.0 is $\frac{1}{10}$ of 0.1
 - (C) 0.1 is $\frac{1}{10}$ of 1.0
 - **D** 1.0 is equal to 0.1

Bee Lengths (in meters)

0.019
0.025
0.014
0.028

SHOW YOUR WORK

Place Value of Decimals

Essential Question How do you read, write, and represent decimals through thousandths?

UNLOCK the Problem TREAL

The Brooklyn Battery Tunnel in New York City is 1.726 miles long. It is the longest underwater tunnel for vehicles in the United States. To understand this distance, you need to understand the place value of each digit in 1.726.

WORLD

You can use a place-value chart to understand decimals. Whole numbers are to the left of the decimal point. Decimals are to the right of the decimal point. The thousandths place is to the right of the hundredths place.

Tens	Ones	Tenths	Hundredths	Thousandths
	1	7	2	6
1	1 × 1	$7 imes rac{1}{10}$	$2 imes rac{1}{100}$	$6 imesrac{1}{1,000}$
	1.0	0.7	0.02	0.006

▲ The Brooklyn Battery Tunnel passes under the East River.

The place value of the digit 6 in 1.726 is thousandths. The value of 6 in 1.726 is $6 \times \frac{1}{1.000}$, or 0.006.

Standard Form: 1.726

Word Form: one and seven hundred twenty-six thousandths

Expanded Form:
$$1 \times 1 + 7 \times \left(\frac{1}{10}\right) + 2 \times \left(\frac{1}{100}\right) + 6 \times \left(\frac{1}{1,000}\right)$$

MATHEMATICAL PRACTICES

Math Talk Explain how the value of the last digit in a decimal can help you read a decimal.

Try This! Use place value to read and write decimals.

A Standard Form: 2.35 Word Form: two and	
Expanded Form: $2 \times 1 +$	
B Standard Form: Word Form: three and six hundred fourteen thousandths	
Expanded Form: $+ 6 \times (\frac{1}{10}) + $	

Example Use a place-value chart.

The silk spun by a common garden spider is about 0.003 millimeter thick. A commonly used sewing thread is about 0.3 millimeter thick. How does the thickness of the spider silk and the thread compare?



STEP 1 Write the numbers in a place-value chart.

Ones	Tenths	Hundredths	Thousandths

STEP 2

Count the number of decimal place-value positions to the digit 3 in 0.3 and 0.003.

0.3 has _____ fewer decimal places than 0.003

2 fewer decimal places: $10 \times 10 =$

0.3 is ______ times as much as 0.003

0.003 is _____ of 0.3

So, the thread is ______ times as thick as the garden spider's silk. The thickness of the garden spider's silk is

that of the thread.

You can use place-value patterns to rename a decimal.

Try This! Use place-value patterns.

Rename 0.3 using other place values.

0. <mark>3</mark> 00	3 tenths	$3 imes rac{1}{10}$
0.300	hundredths	× <u>1</u>
0.300		

Name	
------	--

Share and Show MATH

1. Complete the place-value chart to find the value of each digit.

Ones	Tenths	Hundredths	Thousandths
3	5	2	4
3 × 1		$2 imes rac{1}{100}$	
	0.5		

Write the value of the underlined digit.

2. 0.5<u>4</u>

<u>1</u> 3	3. 6. <u>2</u> 34	€ 4. 3.95 <u>4</u>

.

Write the number in two other forms

5.

6 7 632
0. 7.032
·

On Your Own Write the value of the underlined digit. **7.** 0.4<u>9</u>6 **8.** 2.<u>7</u>26 **9.** 1.06<u>6</u> **10.** 6.<u>3</u>99 **11.** 0.00<u>2</u> **12.** 14.37<u>1</u> Write the number in two other forms. **13.** 0.489 **14.** 5.916

C Houghton Mifflin Harcourt Publishing Company

Problem Solving REAL WORLD

Use the table for 15–17.

- **15.** What is the value of the digit 7 in New Mexico's average annual rainfall?
- **16.** The average annual rainfall in Maine is one and seventy-four thousandths of a meter per year. Complete the table by writing that amount in standard form.
- **17.** Which of the states has an average annual rainfall with the least number in the thousandths place?
- What's the Error? Damian wrote the number four and twenty-three thousandths as 4.23. Describe and correct his error.

19. Write Math Explain how you know that the digit 6 in the numbers 3.675 and 3.756 does not have the same value.

20. Test Prep In 24.736, which digit is in the thousandths place?

(**D**) 7

- 3 **(C)** 6
- **B** 4

Average Annual	Rainfall (in meters)
California	0.564
New Mexico	0.372
New York	1.041
Wisconsin	0.820
Maine	



Compare and Order Decimals

Essential Question How can you use place value to compare and order decimals?

UNLOCK the Problem REAL WORLD

The table lists some of the mountains in the United States that are over two miles high. How does the height of Cloud Mountain in New York compare to the height of Boundary Mountain in Nevada?

Mountain Heights				
Mountain and State	Height (in miles)			
Boundary, Nevada	2.488			
Cloud, New York	2.495			
Grand Teton, Wyoming	2.607			
Wheeler, New Mexico	2.493			



The Tetons are located in Grand Teton National Park.

9

One Way Use place value.

Line up the decimal points. Start at the left. Compare the digits in each place-value position until the digits are different.

STEP 1 Compare the ones. **STEP 2** Compare the tenths. STEP 3 Compare the hundredths. 2.495 2.495 2.495 2 = 2 2.488 2.488 2.488) 8, then 2.495 () 2.488, and 2.488 () 2.495. Since 9 (So, the height of Cloud Mountain is ______ the height of Boundary Mountain.

Another Way Use a place-value chart to compare.

Compare the height of Cloud Mountain to Wheeler Mountain.

Ones	 Tenths 	Hundredths	Thousandths
2	• 4	9	5
2	• 4	9	3
2 = 2 Since 5	4 = 3, then 2.49	9 = 52.493, an	$5 > _$
So, the he of Wheele	ight of Cloud M r Mountain.	ountain is	the h

Order Decimals You can use place value to order decimal numbers.

🚹 Example

Mount Whitney in California is 2.745 miles high, Mount Rainier in Washington is 2.729 miles high, and Mount Harvard in Colorado is 2.731 miles high. Order the heights of these mountains from least to greatest. Which mountain has the least height? Which mountain has the greatest height?

Line up the decimal points. There are	
the same number of ones. Circle the	
tenths and compare.	

2.745	Whitney		

- 2.729 Rainier
- 2.731 Harvard

So, ____

There are the same number of tenths.

1	STEP 2
p the decimal points. There are me number of ones. Circle the	Underline the hundredths and compare. Order from least to greatest.
s and compare.	2.745 Whitney
Whitney	2.729 Rainier
Rainier	2.731 Harvard
Harvard	Since $\bigcirc < \bigcirc < \bigcirc$, the heights in order from least to
are the same number of tenths.	
	greatest are,,,,
has the leas	t height and Math Talk Explain why you do

has the greatest height.

Try This! Use a place-value chart.

What is the order of 1.383, 1.321, 1.456, and 1.32 from greatest to least?

- Write each number in the place-value chart. Compare the digits, beginning with the greatest place value.
- Compare the ones. The ones are the same. •
- Compare the tenths. 4 > 3. •

The greatest number is Circle the greatest number in the place-value chart.

• Compare the remaining hundredths. 8 > 2.

The next greatest number is _____. Draw a rectangle around the number.

• Compare the remaining thousand ths. 1 > 0.

So, the order of the numbers from greatest to least is:

Ones of	• Tenths	Hundredths	Thousandths
1 0	• 3	8	3
1 .	•		
1 .	•		
1 .	•		

not have to compare the digits in

the thousandths place to order the heights of the 3 mountains.

C Houghton Mifflin Harcourt Publishing Company

Name	_
------	---



Problem Solving REAL WORLD

Use the Table for 23–26.

- **23.** In comparing the height of the mountains, which is the greatest place value where the digits differ?
- 24. How does the height of Steele Mountain compare to the height of Blackburn Mountain? Compare the heights using words.



Mountains Over Th	ree Miles High
Mountain and Location	Height (in miles)
Blackburn, Alaska	3.104
Bona, Alaska	3.134
Steele, Yukon	3.152

25. Write Math Explain how to order the height of the mountains from greatest to least.



26. What if the height of Blackburn Mountain were 0.05 mile greater. Would it then be the mountain with the greatest height? Explain.

- 27. Test Prep Mount Logan in the Yukon is 3.702 miles high. Mount McKinley in Alaska is 3.848 miles high and Pico de Orizaba in Mexico is 3.571 miles high. Order these mountains by height from greatest to least.
 - A Logan, McKinley, Pico de Orizaba
 - (B) McKinley, Logan, Pico de Orizaba
 - C Pico de Orizaba, Logan, McKinley
 - D Logan, Pico de Orizaba, McKinley

Round Decimals

Essential Question How can you use place value to round decimals to a given place?

WILOCK the Problem

The Gold Frog of South America is one of the smallest frogs in the world. It is 0.386 of an inch long. What is this length rounded to the nearest hundredth of an inch?

One Way Use a place-value chart.

- Write the number in a place-value chart and circle the digit in the place value to which you want to round.
- In the place-value chart, underline the digit to the right of the place to which you are rounding.
- If the digit to the right is less than 5, the digit in the place value to which you are rounding stays the same. If the digit to the right is 5 or greater, the digit in the rounding place increases by 1.
- Drop the digits after the place to which you are rounding.

So, to the nearest hundredth of an inch, a Gold Frog is

about _____ of an inch long.

Another Way Use place value.

The Little Grass Frog is the smallest frog in North America. It is 0.437 of an inch long.

```
A What is the length of the frog to the nearest hundredth of an inch?
```

```
\begin{array}{cc} 0.437 & \mathsf{7} > \mathsf{5} \\ \downarrow \\ 0.44 \end{array}
```

So,	to	the	nearest	hundredth	of an	inch,	the fro	g

is about ______ of an inch long.

- Underline the length of the Gold Frog.
- Is the frog's length about the same as the length or the width of a large paper clip?



Think: Does the digit in the rounding place stay the same or increase by 1?

B What is the length of the frog to the nearest tenth of an inch?

0.437 3 < 5 ↓ 0.4

So, to the nearest tenth of an inch, the frog is

about ______ of an inch long.

🚹 Example

The Goliath Frog is the largest frog in the world. It is found in the country of Cameroon in West Africa. The Goliath Frog can grow to be 11.815 inches long. How long is the Goliath Frog to the nearest inch?



STEP 1 Write 11.815 in the place-value chart.

Tens	Ones	Tenths	Hundredths	Thousandths
		•		
		· · ·		
STEP 2	Find the	place to	which you wa	int to round.
STEP 3	Underlin to which	e the dig vou are	it to the right rounding. The	t of the place en round.
	Think: Deplace stay	bes the dig the same	git in the round or increase by	ling 1?
So to th				

Explain why any number less than 12.5 and greater than or equal to 11.5 would round to 12 when rounded to the nearest whole number.

Try This! Round. 14.603

A	To the n	earest h	undredth	1:		
	Tens	Ones	Tenths	Hundredths	Thousandths	Circle and underline the digits as you
			•			did above to help you round to the nearest hundredth.
B .	So, 14.6 To the n	603 rour earest w	nded to t	the nearest h	undredth is	·
	Tens	Ones	Tenths	Hundredths	Thousandths	Circle and underline the digits as you
						did above to help you round to the

So, 14.603 rounded to the nearest whole number is _____.

C Houghton Mifflin Harcourt Publishing Company

Name		
Share and Show	derlined digit. Round each erlined digit.	• • • • • • • • • • • • • • • • • • • •
1. 0.6 <u>7</u> 3	∛ 2. 4. <u>2</u> 82	3. 1 <u>2</u> .917
Name the place value to which	each number was rounded.	
4. 0.982 to 0.98	5. 3.695 to 4	● 6. 7.486 to 7.5

.

On Your Own

Write the place value of the underlined digit. Round each number to the place of the underlined digit.

7.	0. <u>5</u> 92	8.	<u>6</u> .518	9.	0.8 <u>0</u> 9
10.	3. <u>3</u> 34	11.	12. <u>0</u> 74	12.	4.4 <u>9</u> 4
Nar	ne the place value to which	each	number was rounded.		
13.	0.328 to 0.33	14.	2.607 to 2.61	15.	12.583 to 13
Rou	and 16.748 to the place nam	ed.			
16.	tenths	17.	hundredths	18.	ones
19.	Write Math > Explain what	at hap	pens when you round 4.999 to		
	the nearest tenth.				

Problem Solving REAL WORLD

Use the table for 20–22.

- **20.** The speeds of two insects when rounded to the nearest whole number are the same. Which two insects are they?
- **21.** What is the speed of the housefly rounded to the nearest hundredth?
- 22. What's the Error? Mark said that the speed of a dragonfly rounded to the nearest tenth was 6.9 meters per second. Is he correct? If not, what is his error?

Insect Speeds (meters per second)
Insect	Speed
Dragonfly	6.974
Horsefly	3.934
Bumblebee	2.861
Honeybee	2.548
Housefly	1.967
	10

SHOW YOUR WORK

23. Write Math A rounded number for the speed of an insect is 5.67 meters per second. What are the fastest and slowest speeds to the thousandths that could round to 5.67? Explain.

24. Test Prep To which place value is the number rounded?

(**D**)

6.706 to 6.71

(A) ones

(R) topt

120

C hundredths

thousandths

B) tenths

FOR MORE PRACTICE: Standards Practice Book, pp. P59–P60

Lesson 3.5

Name _____

Decimal Addition

Essential Question How can you use base-ten blocks to model decimal addition?

CONNECT You can use base-ten blocks to help you find decimal sums.

B. Add the hundredths first by combining them.

Investigate

Materials base-ten blocks



.

0.01 one hundredth

0.1



- **C.** Add the tenths by combining them.
 - Do you need to regroup the tenths? Explain.

A. Use base-ten blocks to model the sum of 0.34 and 0.27.

• Do you need to regroup the hundredths? Explain.

D. Record the sum. 0.34 + 0.27 =

Draw Conclusions

- 1. What if you combine the tenths first and then the hundredths? Explain how you would regroup.
- 2. **Synthesize** If you add two decimals that are each greater than 0.5, will the sum be less than or greater than 1.0? Explain.

Make Connections

You can use a quick picture to add decimals greater than 1.

STEP 1

Model the sum of 2.5 and 2.8 with a quick picture.

STEP 2

Add the tenths.

• Are there more than 9 tenths? ______ If there are more than 9 tenths, regroup.

Add the ones.



STEP 3

Draw a quick picture of your answer. Then record.





Complete the quick picture to find the sum.



Add. Draw a quick picture.

MATHEMATICAL Model • Reason • Make Sense

Problem Solving

8. Robyn and Jim used quick pictures to model 1.85 + 2.73.



• **Explain** how you would help Robyn understand that regrouping is important when adding decimals.

Lesson 3.6

Name _____

Decimal Subtraction

Essential Question How can you use base-ten blocks to model decimal subtraction?

CONNECT You can use base-ten blocks to help you find the difference between two decimals.





0.1

Investigate

Materials base-ten blocks

- **A.** Use base-ten blocks to find 0.84 0.56. Model 0.84.
- **B.** Subtract 0.56. Start by removing 6 hundredths.
 - Do you need to regroup to subtract? Explain.



- **C.** Subtract the tenths. Remove 5 tenths.
- **D.** Record the difference. 0.84 0.56 =

Draw Conclusions

1. What if you remove the tenths first and then the hundredths? Explain how you would regroup.

2. Synthesize If two decimals are both less than 1.0, what do you know about the difference between them? Explain.

Make Connections

You can use quick pictures to subtract decimals that need to be regrouped.

STEP 1

- Use a quick picture to model 2.82 1.47.
- Subtract the hundredths.



STEP 2

- Subtract the tenths.
- Subtract the ones.



STEP 3

Draw a quick picture of your answer. Then record.







Name	
Share and Show MATH	
Complete the quick picture to find the d	lifference.
1. 0.62 - 0.18 =	0 0
Subtract. Draw a quick picture.	
2. 3.41 - 1.74 =	3. $0.84 - 0.57 =$
4. 0.93 - 0.38 =	5. 2.71 - 1.34 =
6. 4.05 − 1.61 =	● 7. 1.37 - 0.52 =
Mathematical practices Explain how you can	
0.81 - 0.46.	

C Houghton Mifflin Harcourt Publishing Company

Problem Solving

8. Antonio left his MathBoard on his desk during lunch. The quick picture below shows the problem he was working on when he left.



Write a problem that can be solved using the quick picture above.

Pose a problem.	Solve your problem.

• **Describe** how you can change the problem by changing the quick picture.

Name	•
------	---

O Houghton Mifflin Harcourt Publishing Company



Concepts and Skills

1. Explain how you can use base-ten blocks to find 1.54 + 2.37.

omplete the sentenc	e.			
2. 0.04 is $\frac{1}{10}$ of		3. 0.06 i	s 10 times as m	uch as
Vrite the value of the	underlined digit.			
4. 6.5 <u>4</u>	5. 0. <u>8</u> 37	6. 8.70 <u>2</u>		7. <u>9</u> .173
compare. Write <, >,	or =.			
ompare. Write <, >, 8. $6.52 \bigcirc 6.520$	or =.	3.598	10. 8.4	63 🔵 8.483
8. $6.52 \bigcirc 6.520$ Write the place value on the place of the place o	or =. 9. 3.589 (of the underlined digit. f the underlined digit.	3.598 Round each	10. 8.4	63 (8.483
2000 2000 2000 2000 2000 2000 2000 200	or =. 9. 3.589 (of the underlined digit. f the underlined digit. 12. 2.576	3.598 Round each	10. 8.4 13. 4.7	63 () 8.483 <u>6</u> 9
2. compare. Write $<, >,$ 8. $6.52 \bigcirc 6.520$ Write the place value of the place of	or =. 9. 3.589 (of the underlined digit. f the underlined digit. 12. <u>2</u> .576	3.598 Round each	10. 8.4 13. 4.7	63 () 8.483 <u>6</u> 9
20208. 6.52 6.520 Vrite the place value of the place value of the place of t	or =. 9. 3.589 (of the underlined digit. f the underlined digit. 12. <u>2</u> .576 o find the sum or difference	3.598 Round each	10. 8.4	63 () 8.483 <u>6</u> 9

Fill in the bubble completely to show your answer.

- **16.** Marco read that a honeybee can fly up to 2.548 meters per second. He rounded the number to 2.55. To which place value did Marco round the speed of a honeybee?
 - $(\widehat{\mathbf{A}})$ ones $(\widehat{\mathbf{C}})$ hundredths
 - (B) tenths (D) thousandths
- **17.** What is the relationship between 0.04 and 0.004?
 - (\mathbf{A}) 0.04 is 10 times as much as 0.004
 - **B** 0.04 is $\frac{1}{10}$ of 0.004
 - **(C)** 0.004 is 10 times as much as 0.04
 - **D** 0.04 is equal to 0.004
- **18.** Jodi drew a quick picture to model the answer for 3.14 1.75. Which picture did she draw?



- **19.** The average annual rainfall in California is 0.564 of a meter per year. What is the value of the digit 4 in that number?
 - (A) 4×1 (C) $4 \times \frac{1}{100}$ (B) $4 \times \frac{1}{10}$ (D) $4 \times \frac{1}{1,000}$
- **20.** Jan ran 1.256 miles on Monday, 1.265 miles on Wednesday, and 1.268 miles on Friday. What were her distances from greatest to least?
 - A 1.268 miles, 1.256 miles, 1.265 miles
 - **B** 1.268 miles, 1.265 miles, 1.256 miles
 - C 1.265 miles, 1.256 miles, 1.268 miles
 - **(D)** 1.256 miles, 1.265 miles, 1.268 miles

Name ___

Estimate Decimal Sums and Differences

Essential Question How can you estimate decimal sums and differences?



Try This! Use rounding to estimate.

A Round to the nearest whole dollar.	B Round to the nearest ten dollars.
Then subtract.	Then subtract.
\$27.95	\$27.95
-\$11.72 _	<u>-\$11.72</u> <u>-</u>
To the nearest dollar,	To the nearest ten dollars,
\$27.95 – \$11.72 is about	\$27.95 – \$11.72 is about

• Do you want an overestimate or an underestimate when you estimate the total cost of items you want to buy? Explain.

Use Benchmarks Benchmarks are familiar numbers used as points of reference. You can use the benchmarks 0, 0.25, 0.50, 0.75, and 1 to estimate decimal sums and differences.



how using rounding or benchmarks to estimate a decimal difference can give you different answers.

132

Name	ATH	
Share and Show	DARD	••••••
Use rounding to estimate.		
1 . 2.34	2 . 10.39	∛ 3 . \$19.75
1.9	- 4.28	+\$ 3.98
+ 5.23		
Use benchmarks to estimate.		
4 . 0.34	∛ 5 . 10.39	Mathematical practices Math Talk Describe the difference
0.1	- 4.28	between an estimate and an exact
0.1		answer.
On Your Own		
$6 \cap 93$	7 7 4 1	8 1468
0.03	7. 7. T I 3. 8.8	993
+0.10	<u> </u>	<u> </u>
Use benchmarks to estimate.		
9. 12.41	10. <i>8</i> .12	11. 9.75
- 6.47	+ 5.52	- 3.47

 Practice: Copy and Solve Use rounding or benchmarks to estimate.

 12. 12.83 + 16.24 13. \$26.92 - \$11.13 14. 9.41 + 3.82

 Estimate to compare. Write < or >.

 15. 2.74 + 4.22 3.13 + 1.87 16. 6.25 - 2.39 9.79 - 3.84

 estimate

 estimate

 estimate

Model • Reason • Make Sense

Problem Solving REAL WORLD

Use the table to solve 17–18. Show your work.

17. For the week of April 4, 1964, the Beatles had the top four songs. About how long would it take to listen to these four songs?

	Top Songs	0-1
Number	Song Title	Song Length (in minutes)
1	"Can't Buy Me Love"	2.30
2	"She Loves You"	2.50
3	"I Want to Hold Your Hand"	2.75
4	"Please Please Me"	2.00

- 18. What's the Error? Isabelle says she can listen to the first three songs in the table in 6 minutes.
- **19. Test Prep** Fran bought sneakers for \$54.26 and a shirt for \$34.34. If Fran started with \$100, about how much money does she have left?
 - **(A)** \$5
 - **B** \$20
 - **(C)** \$35
 - **D** \$80

Connect to Science

Nutrition

Your body needs protein to build and repair cells. You should get a new supply of protein each day. The average 10-year-old needs 35 grams of protein daily. You can find protein in foods like meat, vegetables, and dairy products.

Use estimation to solve.

20. Gina had a scrambled egg, an oat bran muffin, and a cup of low-fat milk for breakfast. About how many grams of protein did Gina have at breakfast?

Grams of Protein per Serving		
Type of Food	Protein (in grams)	
1 scrambled egg	6.75	
1 cup shredded wheat cereal	5.56	
1 oat bran muffin	3.99	
1 cup low-fat milk	8.22	

21. Pablo had a cup of shredded wheat cereal, a cup of low-fat milk, and one other item for breakfast. He had about 21 grams of protein. What was the third item Pablo had for breakfast? O Houghton Mifflin Harcourt Publishing Company

Name _____

Add Decimals

Essential Question How can place value help you add decimals?

WILOCK the Problem

Henry recorded the amount of rain that fell over 2 hours. In the first hour, Henry measured 2.35 centimeters of rain. In the second hour, he measured 1.82 centimeters of rain.

Henry estimated that about 4 centimeters of rain fell in 2 hours. What is the total amount of rain that fell? How can you use this estimate to decide if your answer is reasonable?

Add. 2.35 + 1.82

• Add the hundredths first.

5 hundredths + 2 hundredths = _____ hundredths

Then add the tenths and ones. Regroup as needed.

3 tenths + 8 tenths = _____ tenths. Regroup.

2 ones + 1 one + 1 regrouped one = _____ ones.

• Record the sum for each place value.

Draw a quick picture to check your work.

_hundredths.	
oup as needed.	2.35
Regroup.	+ 1.82

Math Talk Explain how you know

when you need to regroup in a decimal addition problem.

So, _____ centimeters of rain fell.

Since ______ is close to the estimate, 4, the answer is reasonable.

Equivalent Decimals When adding decimals, you can use equivalent decimals to help keep the numbers aligned in each place. Add zeros to the right of the last digit as needed, so that the addends have the same number of decimal places.

Try This! Estimate. Then find the sum.



• Is your answer reasonable? Explain.

Share and Show	MATH. BOARD	•••••••••••••••••
 Estimate. Then find the sum. Estimate: 	2. Estimate:	3. Estimate:
2.5	8.75	2.03
+ 4.6	+ 6.43	+ 7.89
4. Estimate:	 5. Estimate:	
6.34 + 3.8 =	5.63 + 2.6 =	
		MATHEMATICAL PRACTICES Math Talk Explain why it is important to remember to line up the place values in each number when adding or subtracting decimals.

C Houghton Mifflin Harcourt Publishing Company

Name

On Your Own Estimate. Then find the sum. 6. Estimate: 8. Estimate: _____ 7. Estimate: 12.3 19.2 6.8 + 12.68 + 4.9 +7.4 **9.** Estimate: _____ **10.** Estimate: _____ **11.** Estimate: _____ 4.3 + 2.49 =7.86 + 2.9 =9.95 + 0.47 =Find the sum.

- **12.** seven and twenty-five hundredths added to nine and four tenths
- **13.** twelve and eight hundredths added to four and thirty-five hundredths

- **14.** nineteen and seven tenths added to four and ninety-two hundredths
- **15.** one and eighty-two hundredths added to fifteen and eight tenths

Practice: Copy and Solve Find the sum.

 25. A city receives an average rainfall of 16.99 cer in August. One year, during the month of Augu rained 8.33 centimeters by August 15th. Then another 4.65 centimeters through the end of the What was the total rainfall in centimeters for the second secon	worked ntimeters st, it had it rained ne month. e month?	
A 3.68 centimeters		
B 4.68 centimeters		
C 12.98 centimeters		
D 13.98 centimeters		
a. What do you need to find?		
b. What information are you given?		
c. How will you use addition to find the total num of rain that fell?	ber of centimeters	
d. Show how you solved the problem.	e. Fill in the bubble for the correct answer choice above.	
26. Tania measured the growth of her plant each week. The first week, the plant's height measured 2.65 decimeters. During the second week, Tania's plant grew 0.38 decimeter. How tall was Tania's plant at the end of the second week?	27. Maggie had \$35.13. Then her mom gave her \$7.50 for watching her younger brother. How much money does Maggie have now?	

A 2.27 decimeters

B 3.03 decimeters

C 3.23 decimeters

D 3.93 decimeters

138

FOR MORE PRACTICE:

Standards Practice Book, pp. P67–P68

A \$31.63

B \$32.63

(C) \$41.63

D \$42.63

Name _____

Subtract Decimals

Essential Question How can place value help you subtract decimals?



Try This! Use addition to check.

Since subtraction and addition are inverse operations, you can check subtraction by adding.



• Is your answer correct? Explain.

Share and Show	OARD	•
----------------	------	---

Estimate. Then find the difference.

1. Estimate:	2. Estimate:	 3. Estimate:
5.83	4.45	4.03
-2.18	-1.86	-2.25
Find the difference. Check your	answer.	
4. 0.70	5. 13.2	€. 15.8
<u> </u>	- 8.04	- 9.67

C Houghton Mifflin Harcourt Publishing Company

Name

On Your Own.....

Estimate. Then find the difference.



Find the difference. Check your answer.





- three and seventy-two hundredths subtracted from five and eighty-one hundredths
- **14.** one and six hundredths subtracted from eight and thirty-two hundredths

H.O.T. Algebra Write the unknown number for <i>n</i> .			
15. $5.28 - 3.4 = n$	16. $n - 6.47 = 4.32$	17. 11.57 − <i>n</i> = 7.51	
n =	n =	n =	
Practice: Copy and Solve Find the difference.			
18. 8.42 – 5.14	19. 16.46 – 13.87	20. 34.27 – 17.51	
21. 15.83 – 11.45	22. 12.74 – 10.54	23. 48.21 – 13.65	

WILOCK the Problem TREAL WORLD 24. In peanut butter, how many more grams of protein are there than grams of PEANUT BUTTER **Nutrition Facts** carbohydrates? Use the label at the right. Serving Size 2 Tbsp (32.0 g) Amount Per Serving Calories 190 a. What do you need to know? Calories from Fat 190 % Daily Value* Total Fat 16g 25% Saturated Fat 3g 18% Polyunsaturated Fat 4.4g Monounsaturated Fat 7.8g Cholesterol Omg 0% 0% Sodium 5mg Total Carbohydrates 6.2g 2% Dietary Fiber 1.9g 8% Sugars 2.5g 8% b. How will you use subtraction to find how Protein 8.1g *Based on a 2,000 calorie diet many more grams of protein there are than grams of carbohydrates? c. Show how you solved the problem. d. Complete each sentence. The peanut butter has _____ grams of protein. The peanut butter has _____ grams of carbohydrates. There are _____ more grams of protein than grams of carbohydrates in the peanut butter. 26. Test Prep Allie is 158.7 centimeters tall. Her 25. Kyle is building a block tower. Right now the tower stands 0.89 meter tall. How much younger brother is 9.53 centimeters shorter higher does the tower need to be to reach a than she is. How tall is Allie's younger brother? height of 1.74 meters? (A) 159.27 centimeters

(B) 159.23 centimeters

C 149.27 centimeters

(D) 149.17 centimeters

Patterns with Decimals

Essential Question How can you use addition or subtraction to describe a pattern or create a sequence with decimals?

UNLOCK the Problem TREAL

A state park rents canoes for guests to use at the lake. It costs \$5.00 to rent a canoe for 1 hour, \$6.75 for 2 hours, \$8.50 for 3 hours, and \$10.25 for 4 hours. If this pattern continues, how much should it cost Jason to rent a canoe for 7 hours?

WORLD

A sequence is an ordered list of numbers. A term is each number in a sequence. You can find the pattern in a sequence by comparing one term with the next term.



STEP 1

Write the terms you know in a sequence. Then look for a pattern by finding the difference from one term in the sequence to the next.



STEP 2

Write a rule that describes the pattern in the sequence.

Rule:

STEP 3

Extend the sequence to solve the problem.

\$5.00, \$6.75, \$8.50, \$10.25, _____, ____, ____,

So, it should cost ______ to rent a canoe for 7 hours.

• What observation can you make about the pattern in the sequence that will help you write a rule?

Example Write a rule for the pattern in the sequence. Then find the unknown terms in the sequence.			
29.6, 28.3, 27, 25.7,,, 20.5, 19.2			
STEP 1 Look at the first few terms in the sequence.			
Think: Is the sequence increasing or decreasing from one term to the next?			
STEP 2 Write a rule that describes the pattern in the sequence.			
What operation can be used to describe a sequence that increases?			
What operation can be used to describe a sequence that decreases?			
Rule:			
STEP 3 Use your rule to find the unknown terms. Then complete the sequence above.			

• Explain how you know whether your rule for a sequence

would involve addition or subtraction.

Try This!

Write a rule for the sequence. Then find the unknown term.

65.9, 65.3, _____, 64.1, 63.5, 62.9

Rule:_____

B Write the first four terms of the sequence.

/

/

Rule: start at 0.35, add 0.15

,

Name	
Share and Show MATH	
Write a rule for the sequence.	
 0.5, 1.8, 3.1, 4.4, Think: Is the sequence increasing or decreasing? 	∛ 2 . 23.2, 22.1, 21, 19.9,
Rule:	Rule:
Write a rule for the sequence. Then find the unk	nown term.
3. 31.5, 25.2, 18.9,, 6.3	4. 0.25, 0.75,, 1.75, 2.25
Rule:	Rule:
5. 0.3, 1.5,, 3.9, 5.1	● 6. 19.5, 18.8, 18.1, 17.4,
Rule:	Rule:
	Math Talk What operation, other than addition, suggests an increase from one term to the next?
On Your Own	
Write a rule for the sequence. Then find the unk	nown term.
7. 1.8, 4.1,, 8.7, 11	8. 6.85, 5.73, 4.61,, 2.37
Rule:	Rule:
9. 33.4,, 28.8, 26.5, 24.2	10. 15.9, 16.1, 16.3,, 16.7
Rule:	Rule:
Write the first four terms of the sequence.	
11. Rule: start at 10.64, subtract 1.45	12. Rule: start at 0.87, add 2.15
13. Rule: start at 19.3, add 1.8	14. Rule: start at 29.7, subtract 0.4
////	///

Problem Solving REAL WORLD

15. Bren has a deck of cards. As shown below, each card is labeled with a rule describing a pattern in a sequence. Select a card and decide on a starting number. Use the rule to write the first five terms in your sequence.



Sequence: _____, ____, ____,

Write a problem that relates to your sequence and requires the sequence be extended to solve.

Pose a Problem



C Houghton Mifflin Harcourt Publishing Company

Solve your problem.

Problem Solving • Add and Subtract Money

Essential Question How can the strategy *make a table* help you organize and keep track of your bank account balance?

UNLOCK the Problem REAL WORLD

At the end of May, Mrs. Freeman had an account balance of \$442.37. Since then, she has written a check for \$63.92 and made a deposit of \$350.00. Mrs. Freeman says she has \$729.45 in her account. Make a table to determine if Mrs. Freeman is correct.



Read the Problem	S	olve th	e Problen	n
What do I need to find?	Mrs. Freeman's Checkbook			
	May balance			\$442.37
	Check	\$63.92		-\$63.92
What information do I need to use?	Deposit		\$350.00	
How will I use the information?	-	-		
I need to make a table and use the information to	4	-		
	Mrs. Freemar	i's correct l	pala	ince is

1. How can you tell if your answer is reasonable?

Try Another Problem

Nick is buying juice for himself and 5 friends. Each bottle of juice costs \$1.25. How much does 6 bottles of juice cost? Make a table to find the cost of 6 bottles of juice.

Use the graphic below to solve the problem.



Read the Problem	Solve the Problem
What do I need to find?	
What information do I need to use?	
How will I use the information?	
	So, the total cost of 6 bottles of juice is

2. What if Ginny says that 12 bottles of juice cost \$25.00? Is Ginny's

	statement reasonable? Explain.	
3.	3. If Nick had \$10, how many bottles of juice could he buy?	
	Could usolve t	Explain how you use another strategy to his problem.

Share and Show

1. Sara wants to buy a bottle of apple juice from a vending machine. She needs exactly \$2.30. She has the following bills and coins:





Make and complete a table to find all the ways Sara could pay for the juice.

First, draw a table with a column for each type of bill or coin.

Next, fill in your table with each row showing a different way Sara can make exactly \$2.30.

- What if Sara decides to buy a bottle of water that costs \$1.85? What are all the different ways she can make exactly \$1.85 with the bills and coins she has? Which coin must Sara use?
- At the end of August, Mr. Diaz had a balance of \$441.62. Since then, he has written two checks for \$157.34 and \$19.74 and made a deposit of \$575.00. Mr. Diaz says his balance is \$739.54. Find Mr. Diaz's correct balance.

Model • Reason • Make Sense

On Your Own

Use the following information to solve 4–7.

At Open Skate Night, admission is \$3.75 with a membership card and \$5.00 without a membership card. Skate rentals are \$3.00.

- 4. Aidan paid the admission for himself and two friends at Open Skate Night. Aidan had a membership card, but his friends did not. Aidan paid with a \$20 bill. How much change should Aidan receive?
- 5. The Moores and Cotters were at Open Skate Night. The Moores paid \$6 more for skate rentals than the Cotters did. Together, the two families paid \$30 for skate rentals. How many pairs of skates did the Moores rent?
- 6. Jennie and 5 of her friends are going to Open Skate Night. Jennie does not have a membership card. Only some of her friends have membership cards. What is the total amount that Jennie and her friends might pay for admission?

7. Test Prep Sean and Hope each have a membership card for Open Skate Night. Sean has his own skates, but Hope will have to rent skates. Sean gives the clerk \$15 for their admission and skate rental. How much change should he receive?



STRATEGY Act It Out Draw a Diagram

Make a Table Solve a Simpler Problem Work Backward Guess, Check, and Revise

SHOW YOUR WORK

Choose a Method

Essential Question Which method could you choose to find decimal sums and differences?

WILOCK the Problem

At a track meet, Steven entered the long jump. His jumps were 2.25 meters, 1.81 meters, and 3.75 meters. What was the total distance Steven jumped?

To find decimal sums, you can use properties and mental math or you can use paper and pencil.

- Underline the sentence that tells you what you are trying to find.
- Circle the numbers you need to use.
- What operation will you use?



Try This!

In 1924, William DeHart Hubbard won a gold medal with a long jump of 7.44 meters. In 2000, Roman Schurenko won the bronze medal with a jump of 8.31 meters. How much longer was Schurenko's jump than Hubbard's?

A Use place-value.	B Use a calculator.
8.31 -7.44	

So, Schurenko's jump was _____ meter longer than Hubbard's.

• **Explain** why you cannot use the Commutative Property or the Associative Property to find the difference between two decimals.

Share and Show				
1 . 4.19 + 0.58	2 . 9.99 – 4.1	∛ 3 . 5.7 + 2.25 + 1.3		
4 . 28.6 – 9.84	5 . \$15.79+\$32.81	ĕ 38.44 – 25.86		

Name _____

On Your Own

Find the sum or difference.

7. \$18.39 +\$7.56	8. 8.22 – 4.39	9. 93.6 – 79.84	10. 1.82 2.28 <u>+ 2.18</u>
11. 2.35 <u>- 0.16</u>	12. 5.16 + 4.54	13 . 15.3 <u>- 6.53</u>	14. 2.64 <u>+ 8.41</u>
Practice: Copy and So	Ive Find the sum or differe	ence.	
15. 6.3 + 2.98 + 7.7	16. 27.96 - 16.2	17. 12.63 + 15.04	18. 9.24 – 2.68
19. \$18 - \$3.55	20. 9.73 – 2.52	21. \$54.78 + \$43.62	22. 7.25 + 0.25 + 1.5
23. 14.56 - 7.8	24. 3.35 + 1.4 + 3.65	25. \$22.50 - \$8.99	26. 9.77 + 5.54

Model • Reason • Make Sense

SHOW YOUR WORK

Problem Solving REAL WORLD

Use the table to solve 30-32.

- **30.** How much farther did the gold medal winner jump than the silver medal winner?
- 31. Write Math The fourth-place competitor's jump measured 8.19 meters. If his jump had been 0.10 meter greater, what medal would he have received?
 Explain how you solved the problem.

Long Jump Results		
Medal	Distance (in meters)	
Gold	8.34	
Silver	8.24	
Bronze	8.20	

- **32.** In the 2004 Olympics, the gold medalist for the men's long jump had a jump of 8.59 meters. How much farther did the 2004 gold medalist jump compared to the 2008 gold medalist?
- **33.** Jake cuts a length of 1.12 meters from a 3-meter board. How long is the board now?
- **34.** Test Prep In the long jump, Danny's first attempt was 5.47 meters. His second attempt was 5.63 meters. How much farther did Danny jump on his second attempt than on his first?
 - (\mathbf{A}) 11.1 meters (\mathbf{C}) 5.16 meters
 - **B** 10.1 meters **D** 0.16 meter

Vocabulary

Choose the best term from the box.

1. If one hundredth is divided into ten equal parts, each part is

one _____. (p. 105)

2. An ordered list of numbers is called a _____. (p. 143)

Concepts and Skills

3. Explain how the value of a decimal changes as you move to the left or the right in a place-value chart.

Write the place value of the underlined digit. Round each number to the place of the underlined digit.

4. 0.7 <u>3</u> 5	5. <u>9</u> .283	6. 4. <u>0</u> 79
Find the sum or difference.		
7. \$12.87 - \$5.75	8. \$32.64 + \$18.78	9. 9.28 - 0.54
10. 14.36 + 7.87	11. 10.05 – 6.38	12. 3.25 + 6.75 + 8.75
GO Assessment Options		
Unline Chapter lest		Chapter 2 155

Vocabulary
sequence
term
thousandth

Fill in the bubble completely to show your answer.

- **13.** Doug bought a pair of sneakers for \$47.82 and a shirt for \$13.36. If Doug had \$100 before his purchase, about how much money does Doug have left now?
 - **(A)** \$29.00
 - **(B)** \$39.00
 - **(C)** \$48.00
 - **D** \$61.00
- 14. Since September, Mrs. Bishop has written a check for \$178.23 and made a deposit of \$363.82. Her balance was \$660.00. Which amount should Mrs. Bishop's checkbook balance show now?
 - **(A)** \$481.77
 - **B** \$483.77
 - **(C)** \$845.59
 - **D** \$847.59
- **15.** Helen earns \$12 each weekend babysitting her brother. After the third weekend, Helen buys a new CD for \$12.48. How much money does Helen have left after buying the CD?
 - **(A)** \$36.00
 - **B** \$24.00
 - **(C)** \$23.52
 - **D** \$11.52
- 16. Morgan jogged 51.2 kilometers one week. Karen jogged 53.52 kilometers the same week. How many more kilometers did Karen jog that week than Morgan?
 - (A) 48.4 kilometers
 - **B** 12.3 kilometers
 - C 2.32 kilometers
 - D 2.3 kilometers

17. Angelo measured the amount of rain that fell on July 14th. His rain gauge recorded 1.54 centimeters. If 1.73 centimeters fell between July 1st and July 13th, which model shows the total amount of rain that fell from July 1st through July 14th?

- **18.** The Ruby Throated Hummingbird has an average weight of just 4.253 grams. What is its average weight rounded to the nearest tenth?
 - **(A)** 4.3 grams
 - **B** 4.253 grams
 - **(C)** 4.25 grams
 - **D** 4.2 grams

Constructed Response

19. The Smiths are on a summer road trip. They travel 10.9 hours the first day, 8.6 hours the second day, and 12.4 hours the final day. About how may hours does the Smith family travel over the 3-day trip?

Explain how you found your answer.

Performance Task

- **20.** The prices for different beverages and snacks at a snack stand in a park are shown in the table.
- Blair buys a pretzel and fruit juice. Jen buys popcorn and iced tea. Find the difference between the cost of the snacks Blair buys and the cost of the snacks Jen buys.

Park Snacks			
ltem	Price		
Fruit Juice	\$0.89		
Iced Tea	\$1.29		
Lemonade	\$1.49		
Pretzel	\$2.50		
Popcorn	\$1.25		

- B For which two beverages is the difference between the prices the greatest? What is the difference?
- **What if** a frosty beverage was being added to the menu that would cost \$0.20 more than the fruit juice? How much would the frosty beverage cost? **Explain** how you can determine the cost by using mental math.